

Theoretical Overview:

Nucleon spin structure and orbital angular momentum

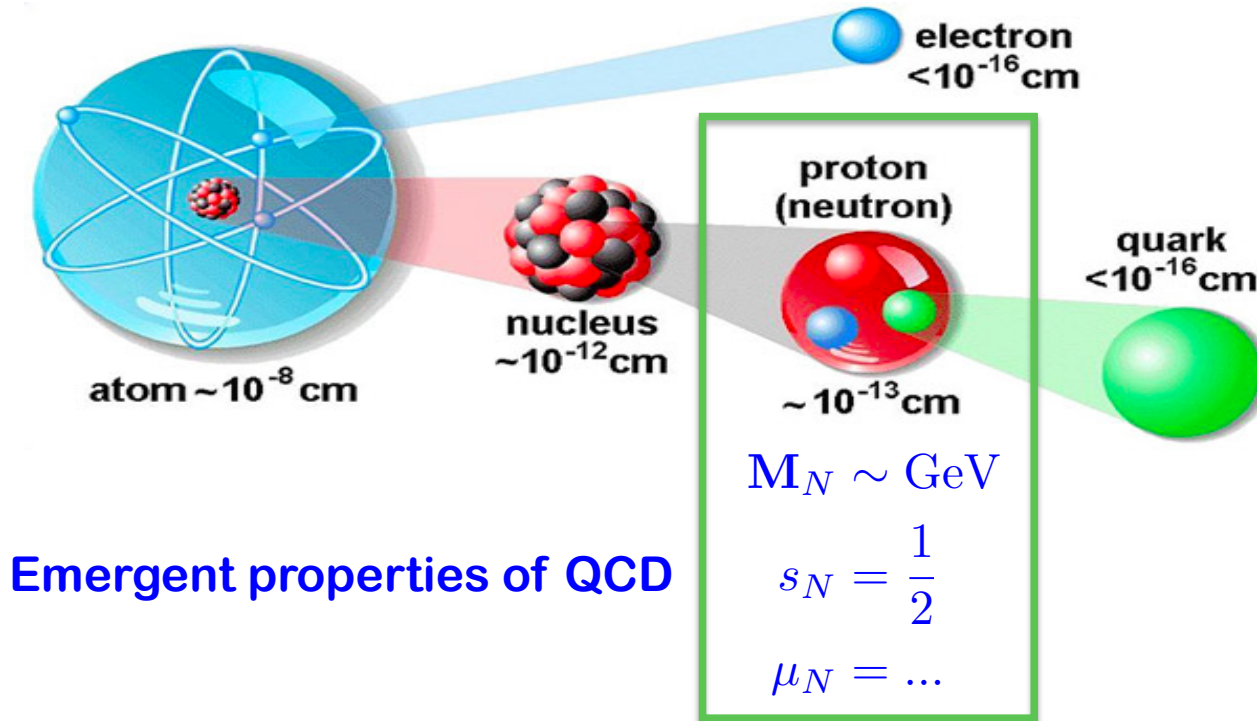
Jian-Wei Qiu

Brookhaven National Laboratory

Acknowledgement: Thanks to those who have provided
valuable inputs, ...

Nucleon spin structure

□ Nucleon: the key building block of the visible matter



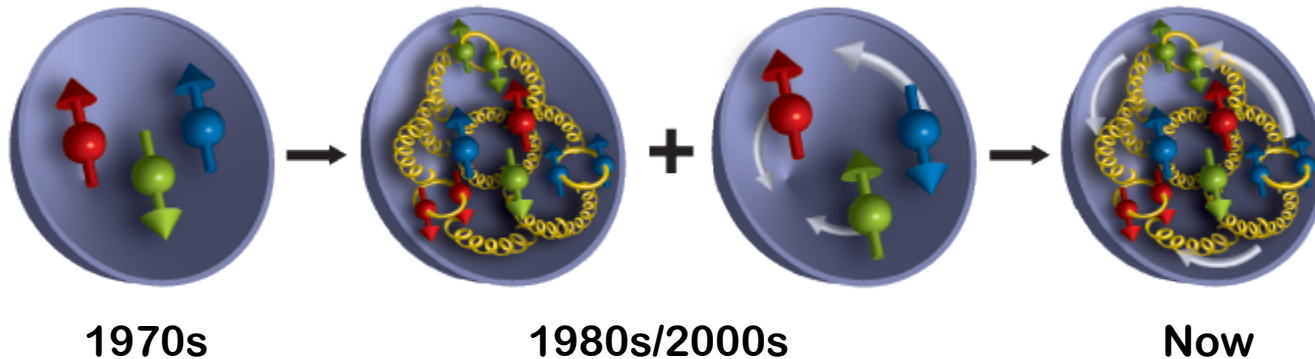
□ 2007 Nuclear Physics Long Range Plan:

“... if we are to claim any understanding of QCD, we must be able to identify how this value (spin=1/2) arises from the nucleon's internal structure.”

What has been done, what needs to be done, and future opportunities?

Nucleon's internal structure

- Our understanding of the nucleon evolves



Nucleon is a strongly interacting, relativistic bound state of quarks and gluons

- QCD bound states:

- ✧ Neither quarks nor gluons appear in isolation!
- ✧ Understanding such systems completely is still beyond the capability of the best minds in the world

- The great intellectual challenge:

Nucleon (spin) structure without “seeing” quarks and gluons?

Nucleon spin structure

□ QCD angular momentum operator:

Jaffe-Manohar, 90
Ji, 96

$$\mathbf{J}^i = \frac{1}{2} \epsilon^{ijk} \int d^3r \mathcal{M}^{0jk}(r)$$

Angular momentum density: $\mathcal{M}^{\mu\alpha\beta}(r)$

□ Transverse polarization:

✧ J_\perp operator does not commute with P^+

✧ Transversely polarized proton is in the eigenstate of transverse Pauli-Lubanski vector, W_\perp

✧ Spin decomposition: $S_\perp = \frac{1}{2} = \sum_f \langle P, S | W_\perp | P, S \rangle \equiv J_q(\mu) + J_g(\mu)$

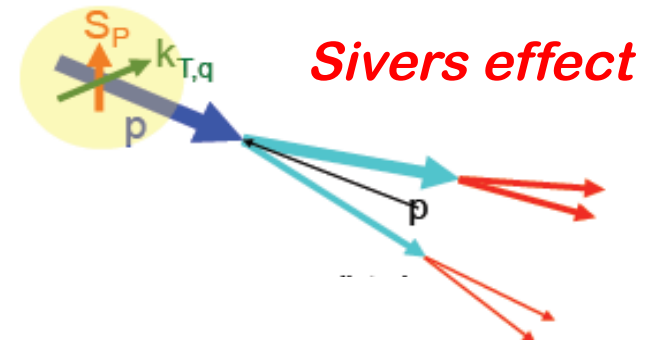
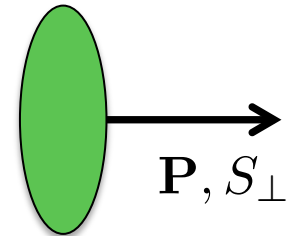
$$J_q = \frac{1}{2} \sum_q \int dx x [q(x) + E_q(x, 0, 0)]$$

Ratcliffe, 98; Burkardt, 2005

in terms of twist-2 quark momentum distribution and twist-2 GPD E

□ Transverse spin physics:

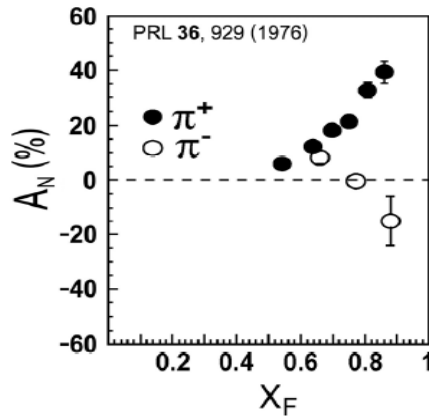
Spin influences parton's motion (TMDs)
as well as its spatial distribution (GPDs)



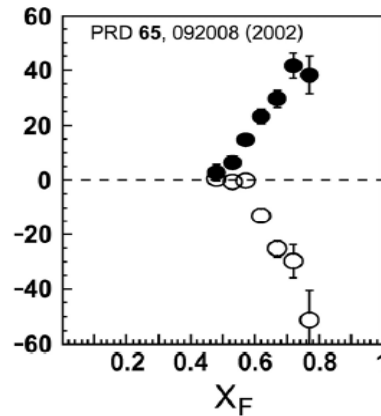
Single transverse-spin asymmetry

□ A_N - consistently observed for over 35 years (~ 0 in parton model)!

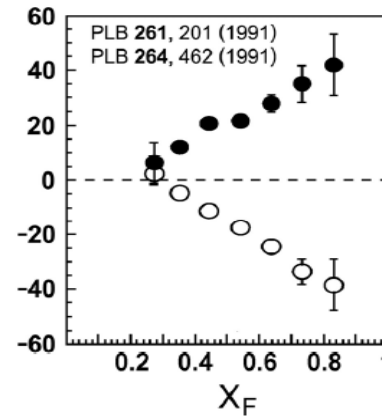
ANL – 4.9 GeV



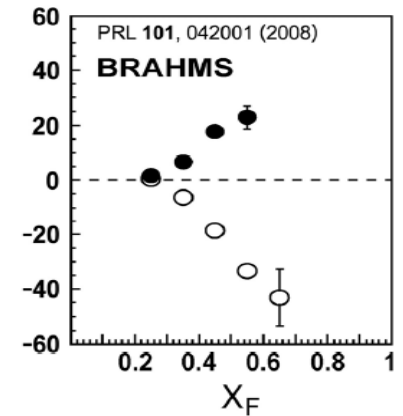
BNL – 6.6 GeV



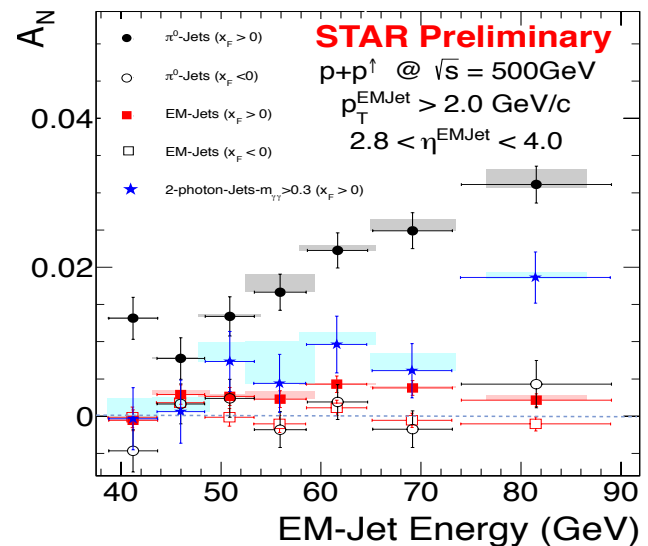
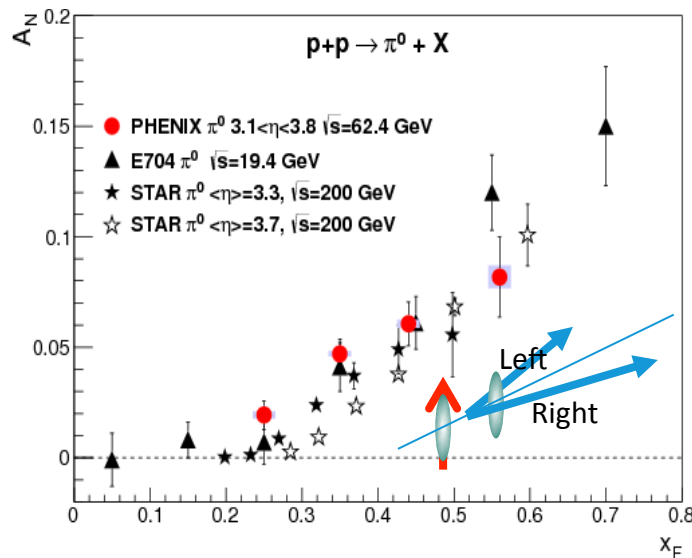
FNAL – 20 GeV



BNL – 62.4 GeV

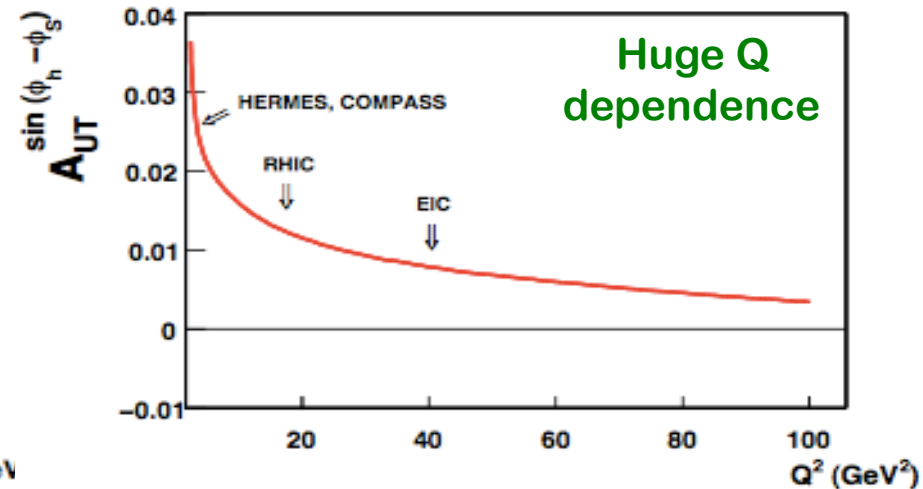
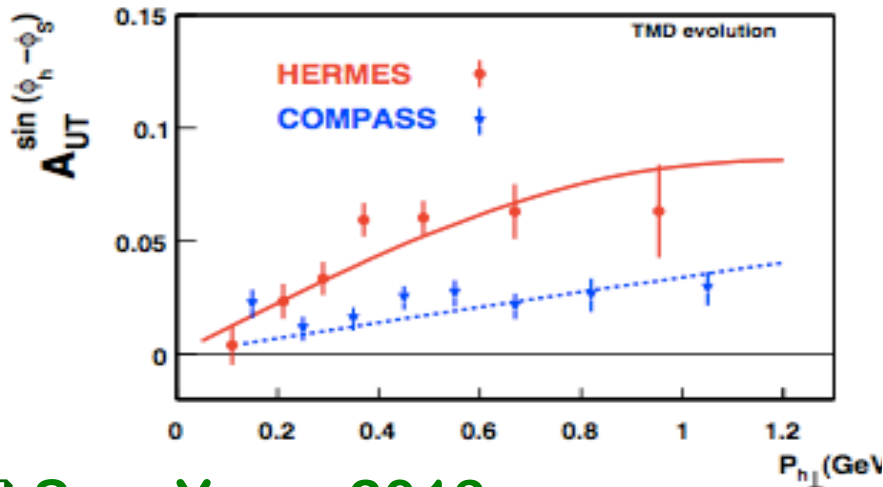


□ Survived the highest RHIC energy:

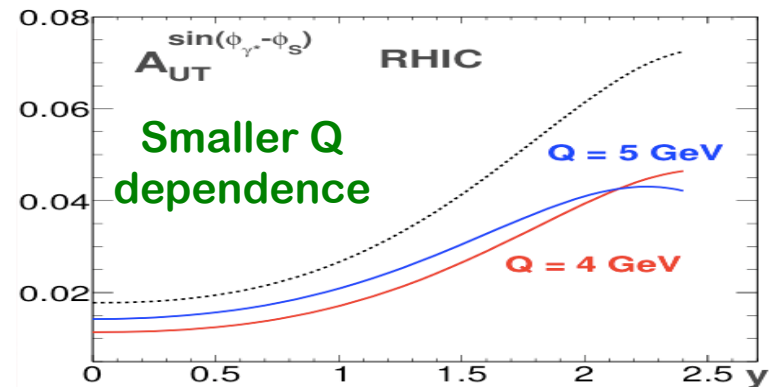
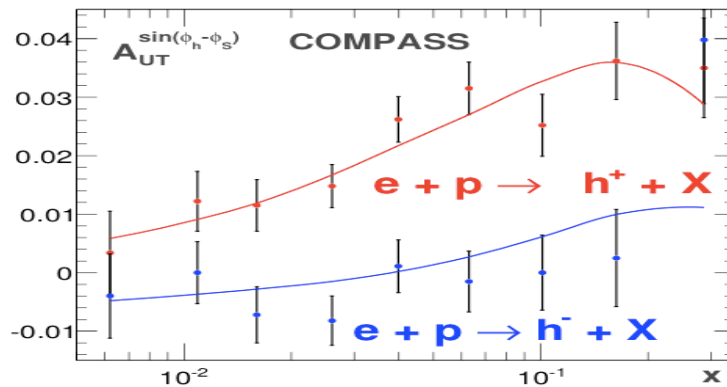


Opportunity: Q^2 -dependence of TMDs

□ Aybat, Prokudin, Rogers, 2012:



□ Sun, Yuan, 2013:



Puzzle: Same evolution equation, but, predicted different Q -dependence?

Evolution equation is in b -space, and sensitive to nucleon (spin) structure !

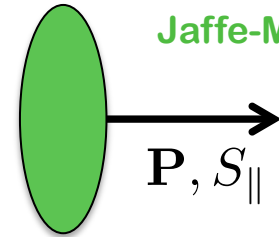
Nucleon spin structure

□ Longitudinal polarization:

$$S_{\parallel}(\mu) = \frac{1}{2} = \sum_f \langle P, S | \mathbf{J}_f^z | P, S \rangle \equiv J_q(\mu) + J_g(\mu)$$

✧ **Quark:** $\mathbf{J}_q = \int d^3r \psi^\dagger(r) [\vec{\gamma} \gamma_5 + (\vec{r} \times i\vec{D})] \psi(r)$

✧ **Gluon:** $\mathbf{J}_g = \int d^3r [\vec{r} \times (\vec{E}(r) \times \vec{B}(r))]$



Jaffe-Manohar, 90
Ji, 96

Neither $J_q(\mu)$, $J_g(\mu)$,
nor $\Delta\Sigma$, L_q , ΔG , L_g ,
are directly observable
Infinite possibilities!

□ Spin decomposition – subtlety:

$$S_{\parallel}(\mu) = \frac{1}{2} \equiv \frac{1}{2} \Delta\Sigma(\mu) + L_q(\mu) + \Delta G(\mu) + [J_g(\mu) - \Delta G(\mu)]$$

[Chen *et al.* (2008)]

[Wakamatsu (2010)]

[Hatta (2011)]

[Lorce (2013)]

Quark helicity

Gluon helicity

$L_g(\mu)$

Quark “orbital” angular momentum

Gluon “orbital” angular momentum

Many possible decompositions – what is the definition of “orbital”?
Mixture of twist-2 and twist-3 – complication in interpretation?

Spin decomposition

□ The “big” question:

If there are infinite possibilities, why bother and what do we learn?

□ The “origin” of the difficulty/confusion:

QCD is a gauge theory: a pure quark field in one gauge is a superposition of quarks and gluons in another gauge

□ The fact:

None of the items in all spin decompositions are **direct** physical observables, unlike cross sections, asymmetries, ...


□ Ambiguity in interpretation – two old examples:

✧ Factorization scheme:

$$F_2(x, Q^2) = \sum_{q, \bar{q}} C_q^{\text{DIS}}(x, Q^2/\mu^2) \otimes q^{\text{DIS}}(x, \mu^2) \quad \text{No glue contribution to } F_2?$$

✧ Anomaly contribution to longitudinal polarization:

$$g_1(x, Q^2) = \sum_{q, \bar{q}} \tilde{C}_q^{\text{ANO}} \otimes \Delta q^{\text{ANO}} + \tilde{C}_g^{\text{ANO}} \otimes \Delta G^{\text{ANO}}$$


 $\Delta \Sigma \longrightarrow \Delta \Sigma^{\text{ANO}} - \frac{n_f \alpha_s}{2\pi} \Delta G^{\text{ANO}}$

Larger quark helicity?

Spin decomposition

□ Key for a good decomposition – sum rule:

- ✧ Every term can be related to a physical observable with controllable approximation – “independently measurable”

DIS scheme is ok for F_2 , but, less effective for other observables

Additional symmetry constraints, leading to “better” decomposition?

- ✧ Natural physical interpretation for each term – “hadron structure”
- ✧ Hopefully, calculable in lattice QCD – “numbers w/o distributions”

The most important task is,

Finding the connection to physical observables!

Quark and gluon helicity contribution

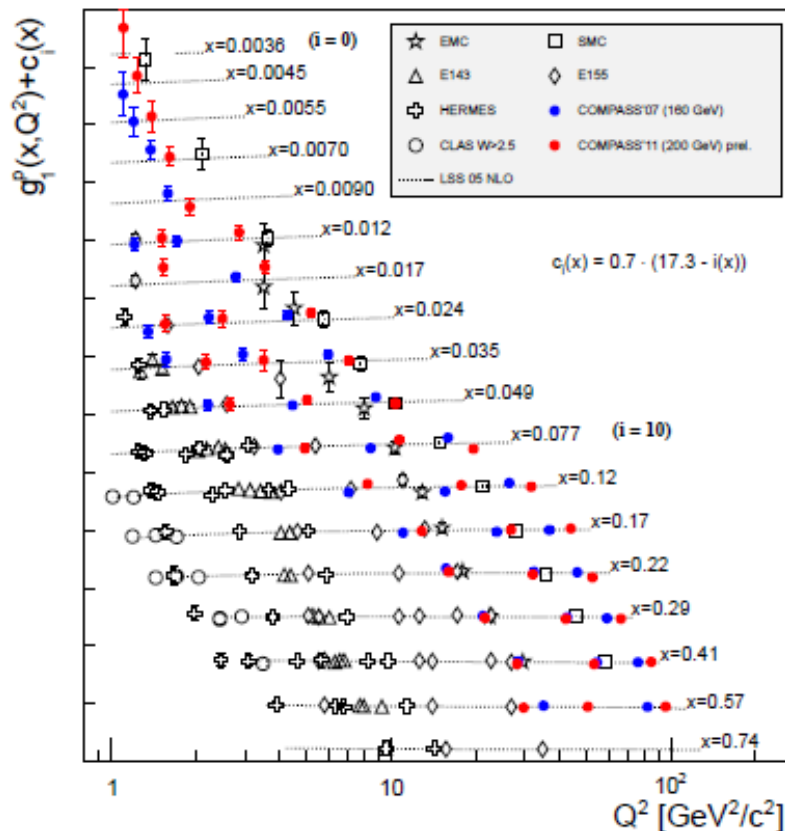
□ QCD Factorization at the leading power:

Link the helicity distributions to the longitudinal spin asymmetries

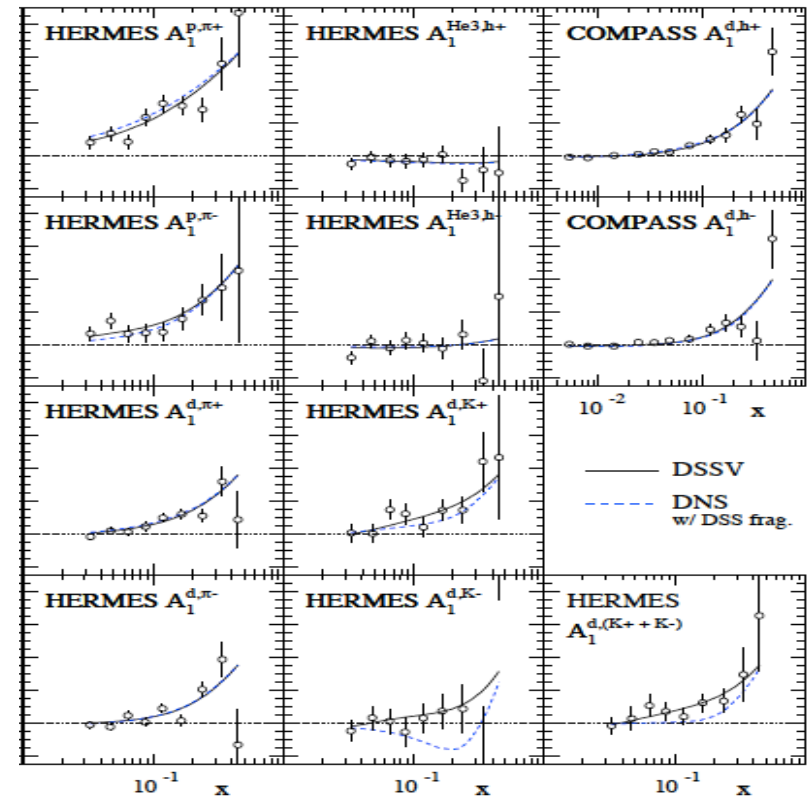
□ Improved data since 2007:

See Seidl's talk

Inclusive DIS



Semi-Inclusive DIS



Quark and gluon helicity contribution

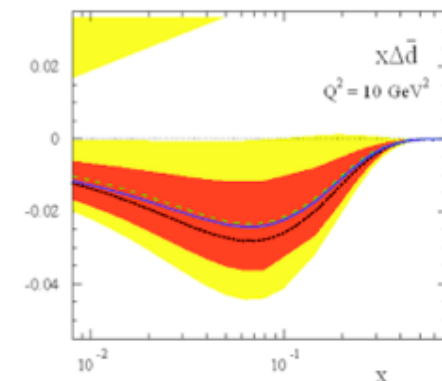
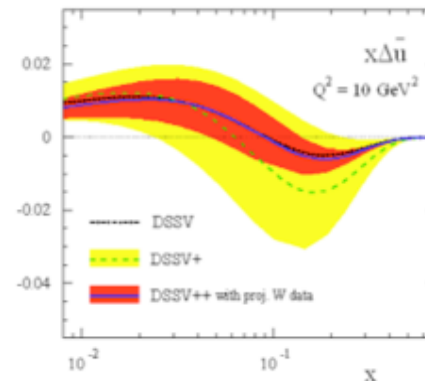
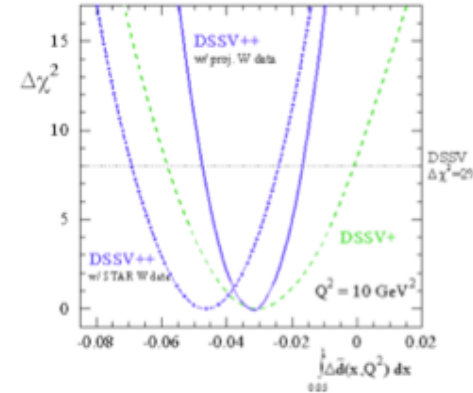
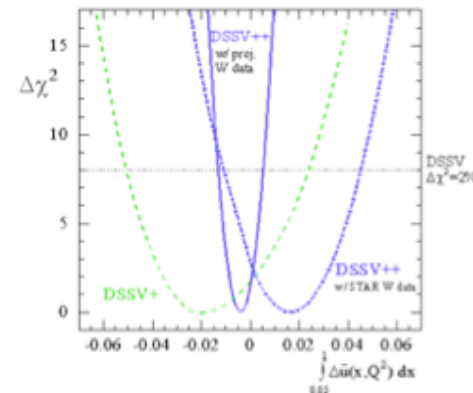
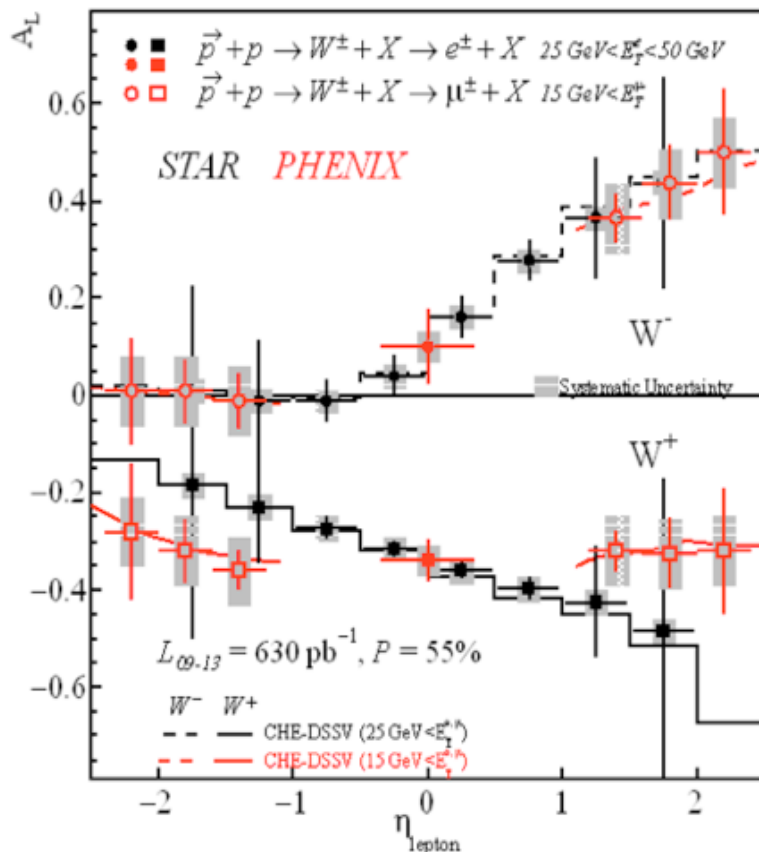
QCD Factorization at the leading power:

Link the helicity distributions to the longitudinal spin asymmetries

Improved data since 2007:

See Seidl's talk

W-production at RHIC – sea flavor separation:



Quark and gluon helicity contribution

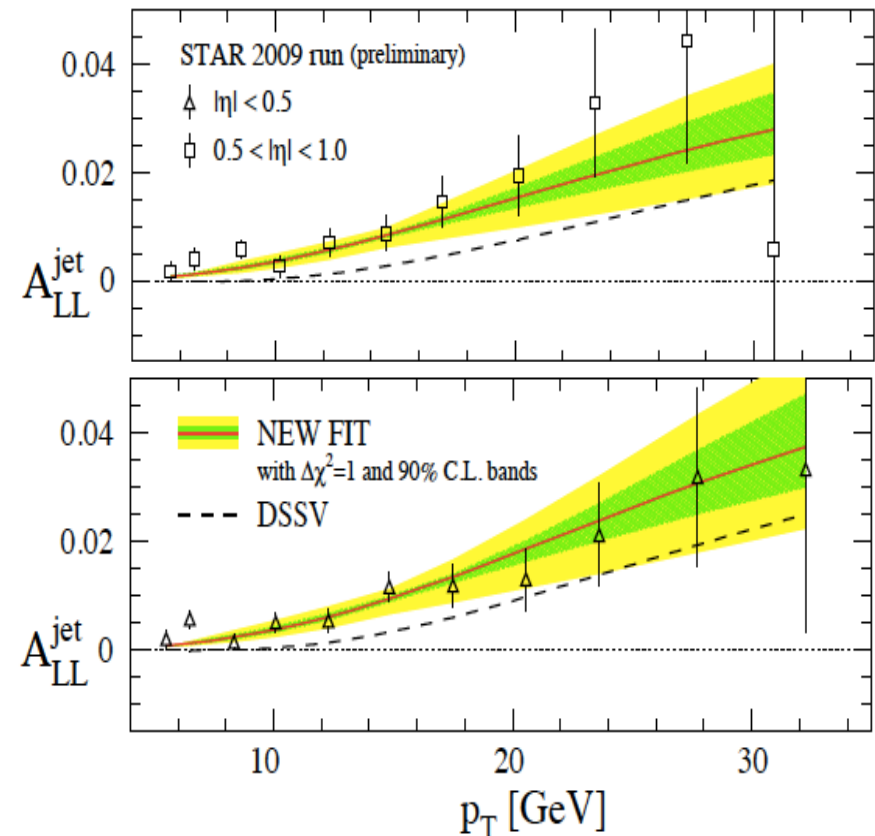
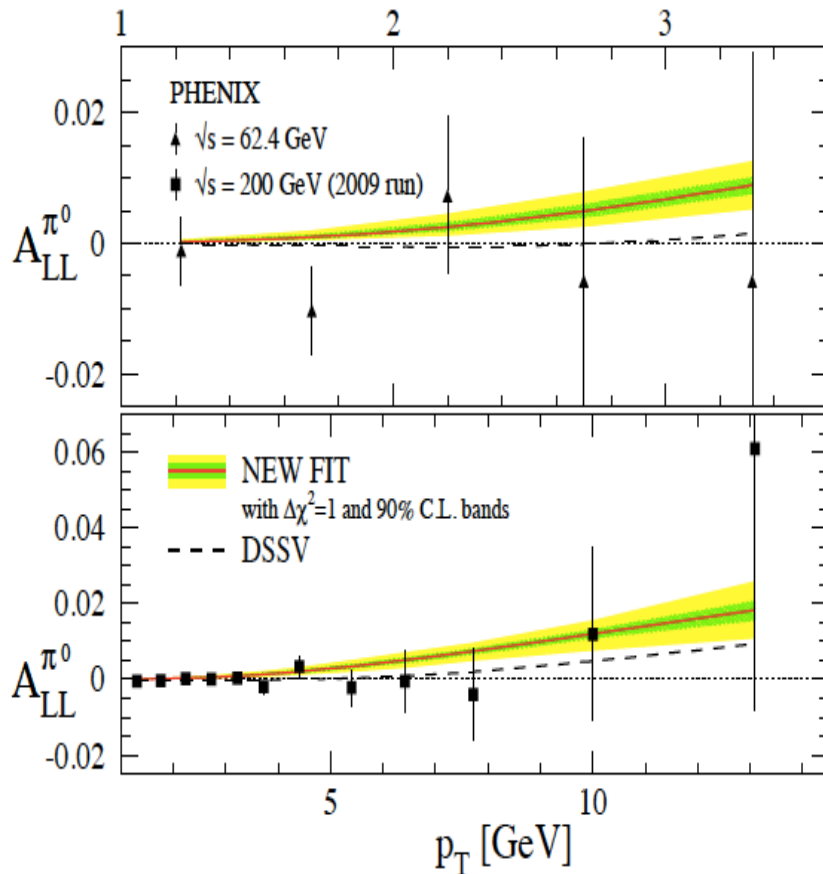
□ QCD Factorization at the leading power:

Link the helicity distributions to the longitudinal spin asymmetries

□ Improved data since 2007:

See Seidl's talk

Jet/pion production at RHIC – gluon helicity:



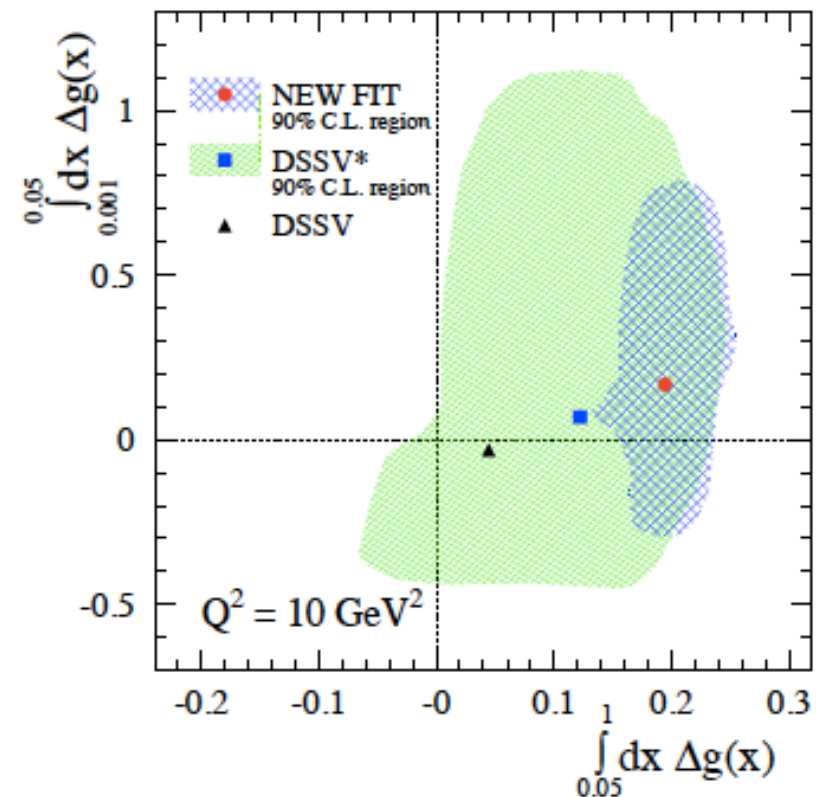
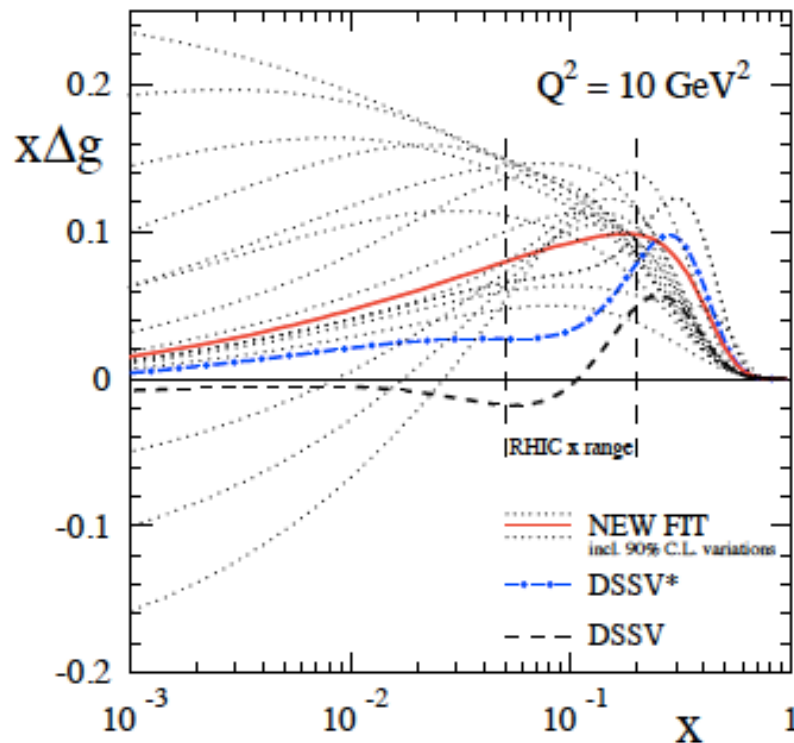
Quark and gluon helicity contribution

□ QCD Factorization at the leading power:

Link the helicity distributions to the longitudinal spin asymmetries

□ Impact on gluon helicity:

de Florian, et al. 1404.4293



- ✧ Red line is the new fit
- ✧ Dotted lines = other fits with 90% C.L.

- ✧ 90% C.L. areas
- ✧ Leads ΔG to a positive #

Quark and gluon helicity contribution

□ QCD Factorization at the leading power:

Link the helicity distributions to the longitudinal spin asymmetries

□ Quark helicity at $x \sim 1$:

Roberts et al, 2013
See also Peng's talk

	$\frac{F_2^n}{F_2^p}$	$\frac{d}{u}$	$\frac{\Delta d}{\Delta u}$	$\frac{\Delta u}{u}$	$\frac{\Delta d}{d}$	A_1^n	A_1^p
DSE-1	0.49	0.28	-0.11	0.65	-0.26	0.17	0.59
DSE-2	0.41	0.18	-0.07	0.88	-0.33	0.34	0.88
$0_{[ud]}^+$	$\frac{1}{4}$	0	0	1	0	1	1
NJL	0.43	0.20	-0.06	0.80	-0.25	0.35	0.77
SU(6)	$\frac{2}{3}$	$\frac{1}{2}$	$-\frac{1}{4}$	$\frac{2}{3}$	$-\frac{1}{3}$	0	$\frac{5}{9}$
CQM	$\frac{1}{4}$	0	0	1	$-\frac{1}{3}$	1	1
pQCD	$\frac{3}{7}$	$\frac{1}{5}$	$\frac{1}{5}$	1	1	1	1

Extremely sensitive to the nucleon's partonic structure and internal spin correlation!

Big difference between two approximations of the DSE treatments

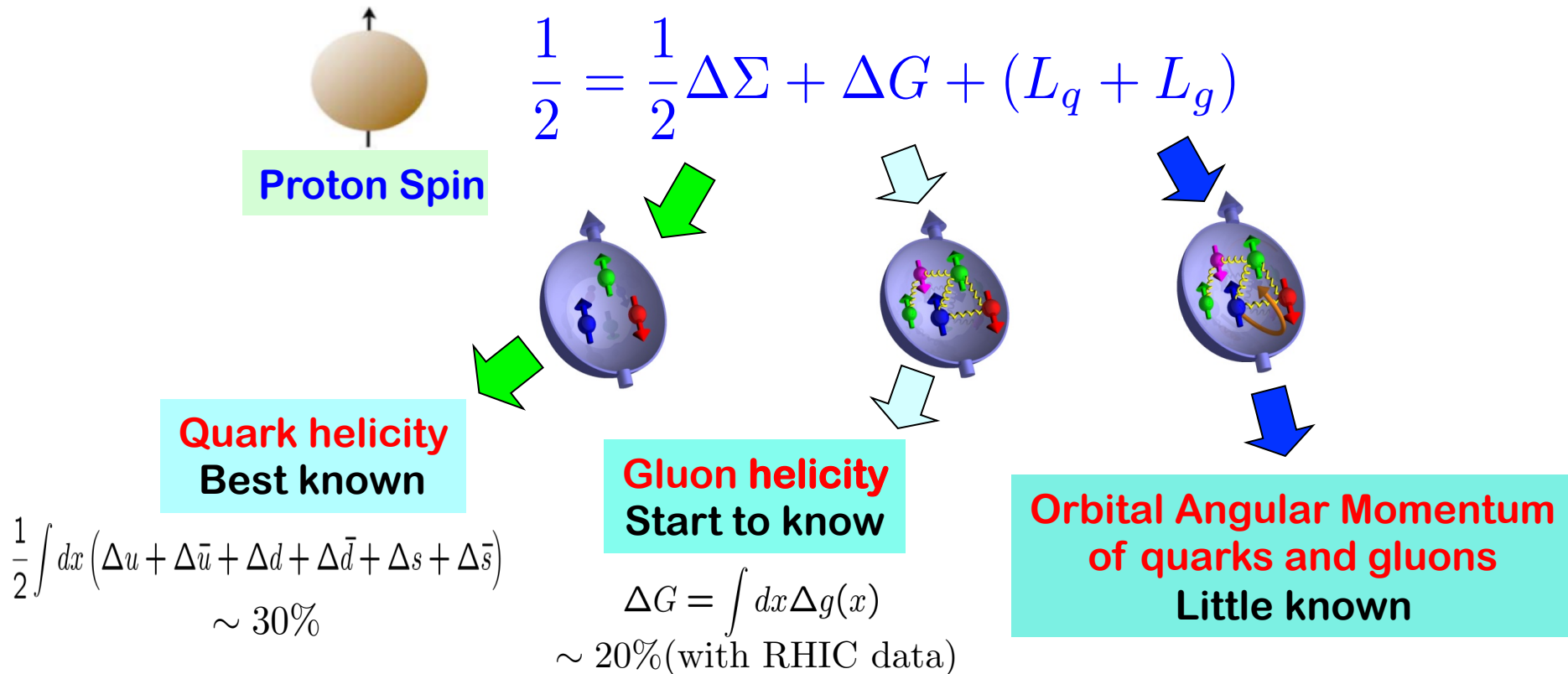
Quark and gluon helicity contribution

□ QCD Factorization at the leading power:

Link the helicity distributions to the longitudinal spin asymmetries

□ Improved knowledge since 2007:

See Ji's talk



OAM: Definitions, ambiguities, connection to observables, ...

Orbital angular momentum contribution

□ An obvious definition:

$$L = L_q + L_g = \frac{1}{2} - \left[\frac{1}{2} \Delta\Sigma + \Delta G \right] \text{Total helicity contribution}$$

$\Delta\Sigma, \Delta G$: Defined by QCD collinear factorization

□ We need to know more than the number!

- ✧ How is the number generated by the dynamics and the structure?
- ✧ Relative role of quarks and gluons in generating the number?
- ✧ ...

□ Two recent workshops:

- ✧ ECT* workshop on “Spin and Orbital Angular Momentum of Quarks and Gluons in the Nucleon” [<http://www.ectstar.eu/node/787>]
- ✧ JLab workshop on “Informal Pre-Town Meeting” [<http://www.jlab.org/conferences/pretownjlab2014/index.html>]

See also talks by Ji, Metz, Meiziani, Peng, and Seidl at this meeting

Orbital angular momentum contribution

□ The definition in terms of Wigner function:

Ji, Xiong, Yuan, PRL, 2012
Lorce, Pasquini, PRD, 2011
Lorce, et al, PRD, 2012

✧ Gauge invariant:

$$L_q \equiv \frac{\langle P, S | \int d^3r \bar{\psi}(\vec{r}) \gamma^+ (\vec{r}_\perp \times i \vec{D}_\perp) \psi(\vec{r}) | P, S \rangle}{\langle P, S | P, S \rangle} = \int (\vec{b}_\perp \times \vec{k}_\perp) W_{FS}(x, \vec{b}_\perp, \vec{k}_\perp) dx d^2\vec{b}_\perp d^2\vec{k}_\perp$$

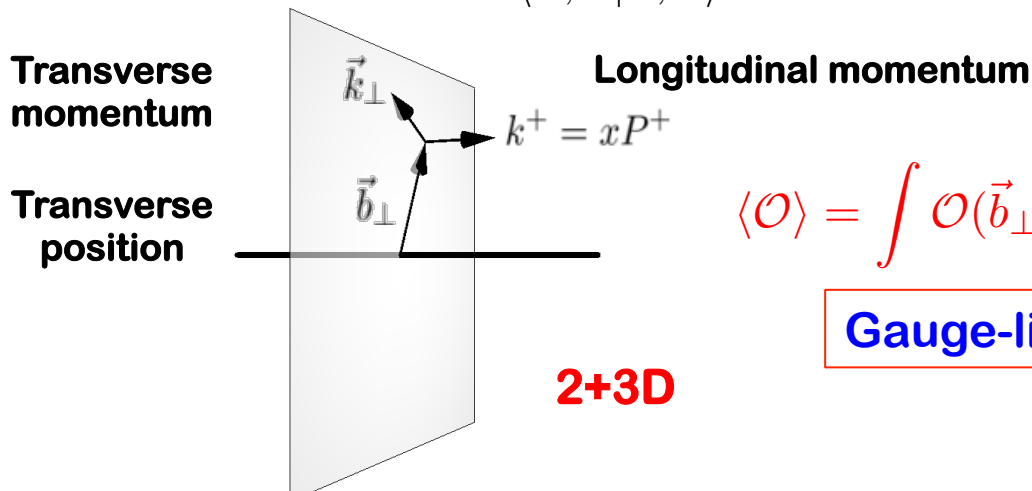
✧ Canonical:

$$l_q \equiv \frac{\langle P, S | \int d^3r \bar{\psi}(\vec{r}) \gamma^+ (\vec{r}_\perp \times i \vec{\partial}_\perp) \psi(\vec{r}) | P, S \rangle}{\langle P, S | P, S \rangle} = \int (\vec{b}_\perp \times \vec{k}_\perp) W_{LC}(x, \vec{b}_\perp, \vec{k}_\perp) dx d^2\vec{b}_\perp d^2\vec{k}_\perp$$

✧ Gauge-dependent potential angular momentum – the difference:

$$l_{q,pot} \equiv \frac{\langle P, S | \int d^3r \bar{\psi}(\vec{r}) \gamma^+ (\vec{r}_\perp \times (-g \vec{A}_\perp)) \psi(\vec{r}) | P, S \rangle}{\langle P, S | P, S \rangle} = L_q - l_q$$

Quark-gluon correlation



$$\langle \mathcal{O} \rangle = \int \mathcal{O}(\vec{b}_\perp, \vec{k}_\perp) W_{GL}(x, \vec{b}_\perp, \vec{k}_\perp) dx d^2\vec{b}_\perp d^2\vec{k}_\perp$$

Gauge-link dependent Wigner function

Same for gluon OAM

Orbital angular momentum contribution

□ The Wigner function:

Ji, Xiong, Yuan, PRL, 2012
Lorce, Pasquini, PRD, 2011
Lorce, et al, PRD, 2012

✧ Quark:

$$W_{GL}^q(x, \vec{k}_\perp, \vec{b}_\perp) = \int \frac{d^2\Delta_\perp}{(2\pi)^2} e^{-i\vec{\Delta}_\perp \cdot \vec{b}_\perp} \int \frac{dz^- d\vec{z}_\perp}{(2\pi)^3} e^{ik \cdot z} \left\langle P + \frac{\vec{\Delta}_\perp}{2} \left| \bar{\Psi}_{GL} \left(-\frac{z}{2} \right) \gamma^+ \Psi_{GL} \left(\frac{z}{2} \right) \right| P - \frac{\vec{\Delta}_\perp}{2} \right\rangle$$

GL: gauge link dependence

Gauge to remove “GL”

$$\Psi_{FS}(z) = \mathcal{P} \left[\exp \left(-ig \int_0^\infty d\lambda z \cdot A(\lambda z) \right) \right] \psi(z)$$

$$\Psi_{LC}(z) = \mathcal{P} \left[\exp \left(-ig \int_0^\infty d\lambda n \cdot A(\lambda n + z) \right) \right] \psi(z)$$

Fock-Schwinger

Light-cone

✧ Gluon:

$$W_{GL}^g(x, \vec{k}_\perp, \vec{b}_\perp) = \int \frac{d^2\Delta_\perp}{(2\pi)^2} e^{-i\vec{\Delta}_\perp \cdot \vec{b}_\perp} \int \frac{dz^- d\vec{z}_\perp}{(2\pi)^3} e^{ik \cdot z} \left\langle P + \frac{\vec{\Delta}_\perp}{2} \left| \mathbf{F}_{GL}^{i+} \left(-\frac{z}{2} \right) \mathbf{F}_{GL}^{+i} \left(\frac{z}{2} \right) \right| P - \frac{\vec{\Delta}_\perp}{2} \right\rangle$$

□ Gauge-invariant extension (GIE):

$$i\vec{\partial}_\perp^\alpha = i\vec{D}_\perp^\alpha(\xi) + \int_{\xi^-}^{\xi^-} d\eta^- L_{[\xi^-, \eta^-]} gF^{+\alpha}(\eta^-, \xi_\perp) L_{[\eta^-, \xi^-]} \quad \text{Twist-3 correlators}$$

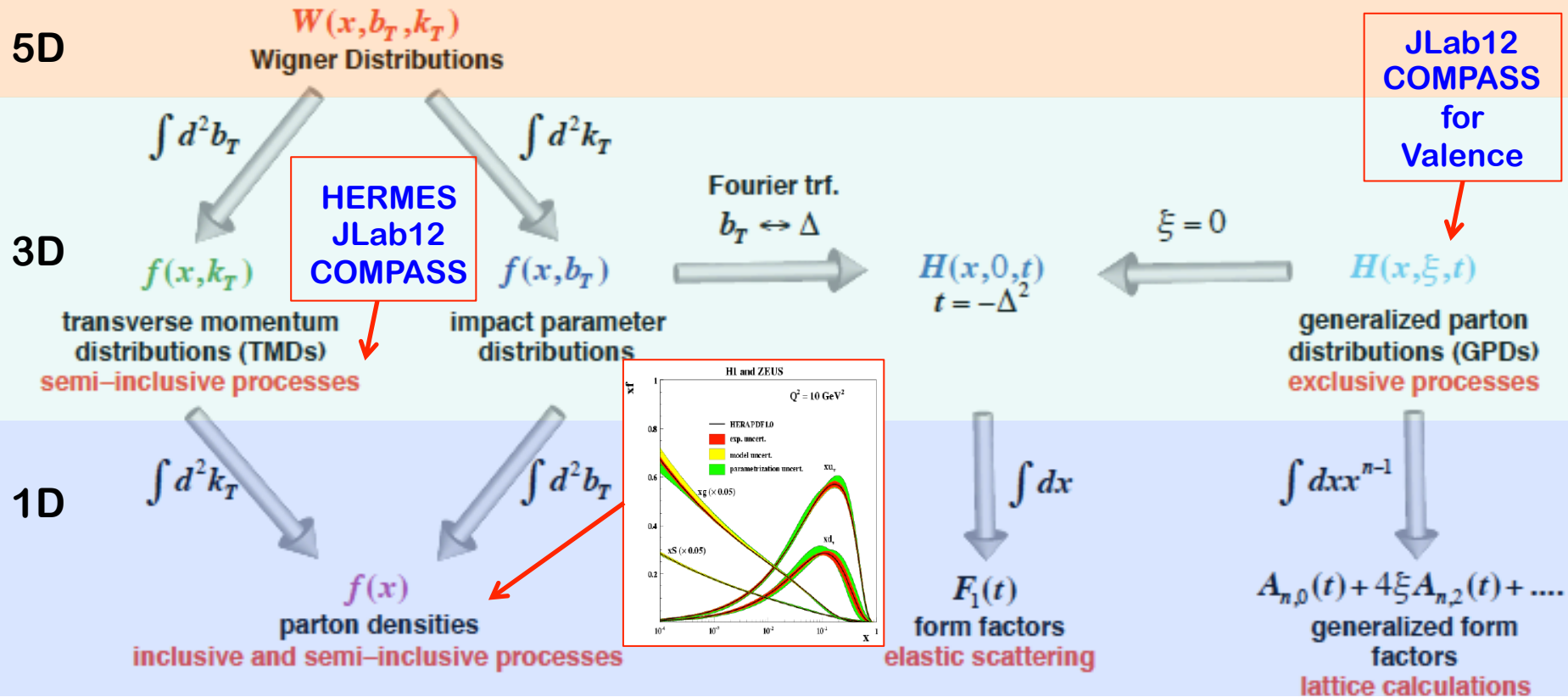
Fixed gauge local operators \longleftrightarrow gauge invariant non-local operators

*Note: the 2+3D Wigner distributions are not “physical”
But, their reduced distributions could be connected to observables*

Unified view of nucleon structure

□ Wigner distributions:

Belitsky, Ji and Yuan, 2004
EIC White Paper, 2012



□ Major advances since 2007:

- ✧ TMDs – Correlation between hadron properties (spin) and parton motion
- ✧ GPDs – Hadron properties (spin) influence parton spatial distribution

Generalized TMDs (GTMDs)

□ The definition:

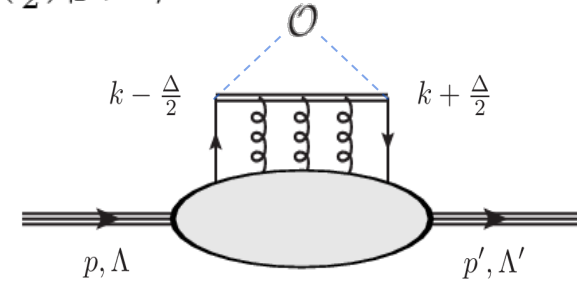
Meissner, et al. 2008
See talk by Metz
Also, Lorce at ECT*

$$W_{\Lambda'\Lambda}^{\mathcal{O}}(P, k, \Delta; \mathcal{W}) = \frac{1}{2} \int \frac{d^4 z}{(2\pi)^4} e^{ik \cdot z} \langle p', \Lambda' | \bar{\psi}(-\frac{z}{2}) \mathcal{W} \mathcal{O} \psi(\frac{z}{2}) | p, \Lambda \rangle$$

□ Connection to the Wigner distribution:

2D FT of GTMDs ($\Delta_{\perp} \rightarrow b_{\perp}$)

$$\rho_{\Lambda'\Lambda}^{\mathcal{O}}(P, k, \vec{b}_{\perp}; \mathcal{W}) = \int \frac{d^2 \Delta_{\perp}}{(2\pi)^2} e^{-i\vec{\Delta}_{\perp} \cdot \vec{b}_{\perp}} W_{\Lambda'\Lambda}^{\mathcal{O}}(P, k, \Delta; \mathcal{W})|_{\Delta^+=0}$$



□ Canonical OAM:

2+3D phase-space density

$$l_q^3 = \int d^2 b_{\perp} [\vec{b}_{\perp} \times \langle \vec{k}_{\perp} \rangle (\vec{b}_{\perp})] = - \int dx d^2 k_{\perp} \frac{\vec{k}_{\perp}^2}{M^2} F_{14}(x, 0, \vec{k}_{\perp}, \vec{0}_{\perp}) \quad \leftarrow \boxed{\text{GTMD}}$$

Spatial distribution of $\langle \vec{k}_{\perp} \rangle$:

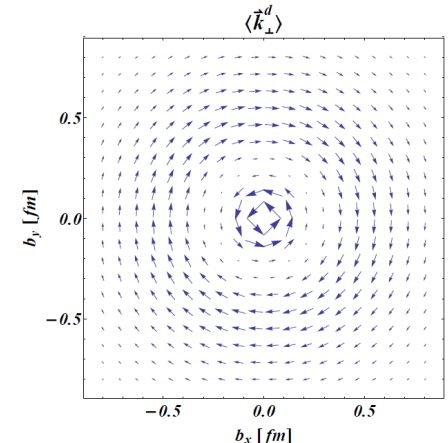
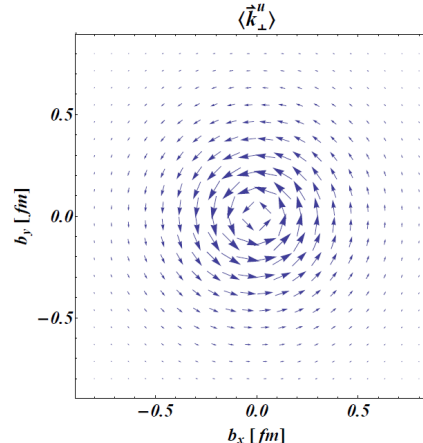
$$\langle \vec{k}_{\perp} \rangle (\vec{b}_{\perp}) = \int d^4 k \vec{k}_{\perp} \rho_{\Lambda'\Lambda}^{\gamma^+}(P, k, \vec{b}_{\perp}; \mathcal{W})$$

[C.L., Pasquini (2011)]

[C.L., Pasquini, Xiong, Yuan (2012)]

[Hatta (2012)]

[Kanazawa, et al. (2014)]



Nucleon spin and OAM from lattice QCD

□ QCD sum rule:

$$S(\mu) = \sum_f \langle P, S | \hat{J}_f^z(\mu) | P, S \rangle = \frac{1}{2} \equiv J_q(\mu) + J_g(\mu)$$

By Local matrix elements
– Lattice QCD

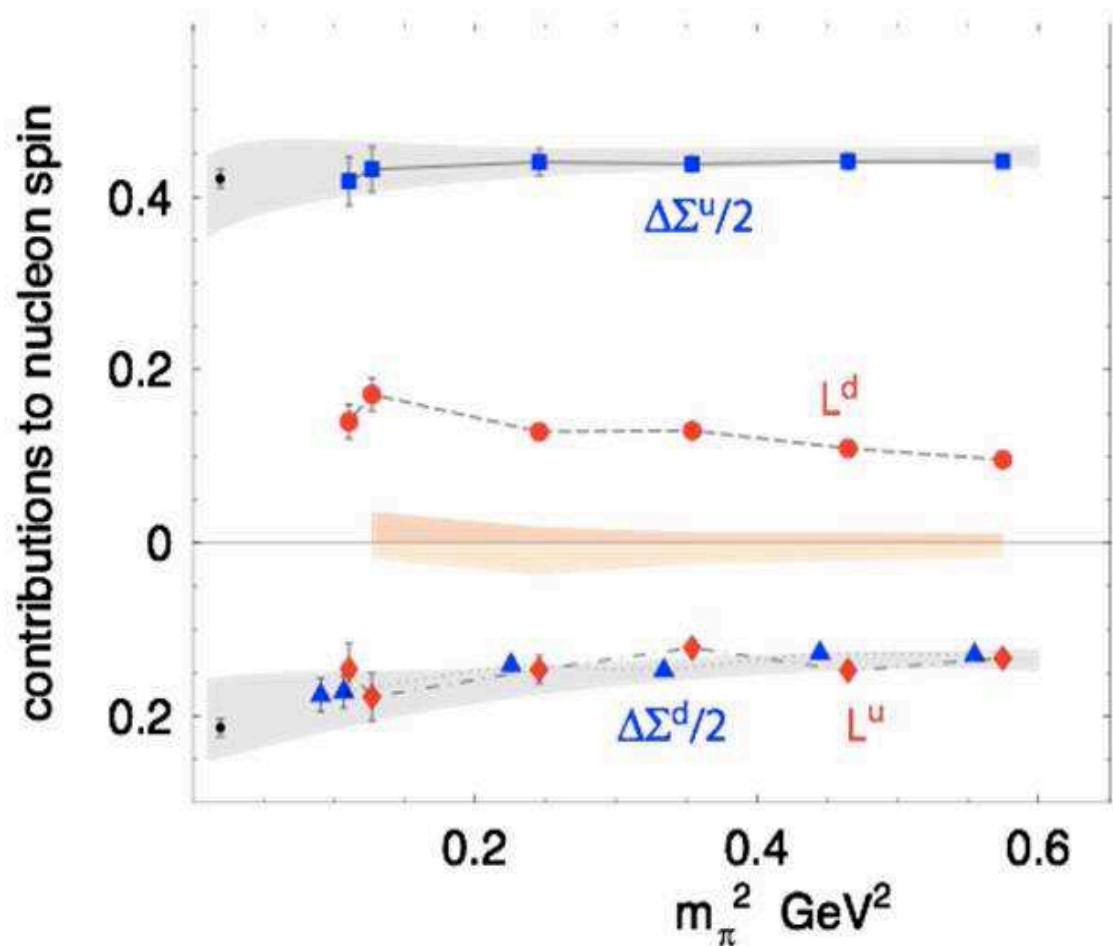
□ Early Lattice result:

$$L_q^z = J_q^z - \frac{1}{2} \Delta q$$

Both L_u and L_d large,

but, $L_u + L_d \sim 0$

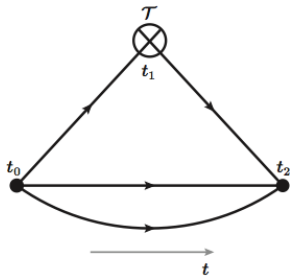
Note: no disconnected
quark loops included
(K.-F. Liu)



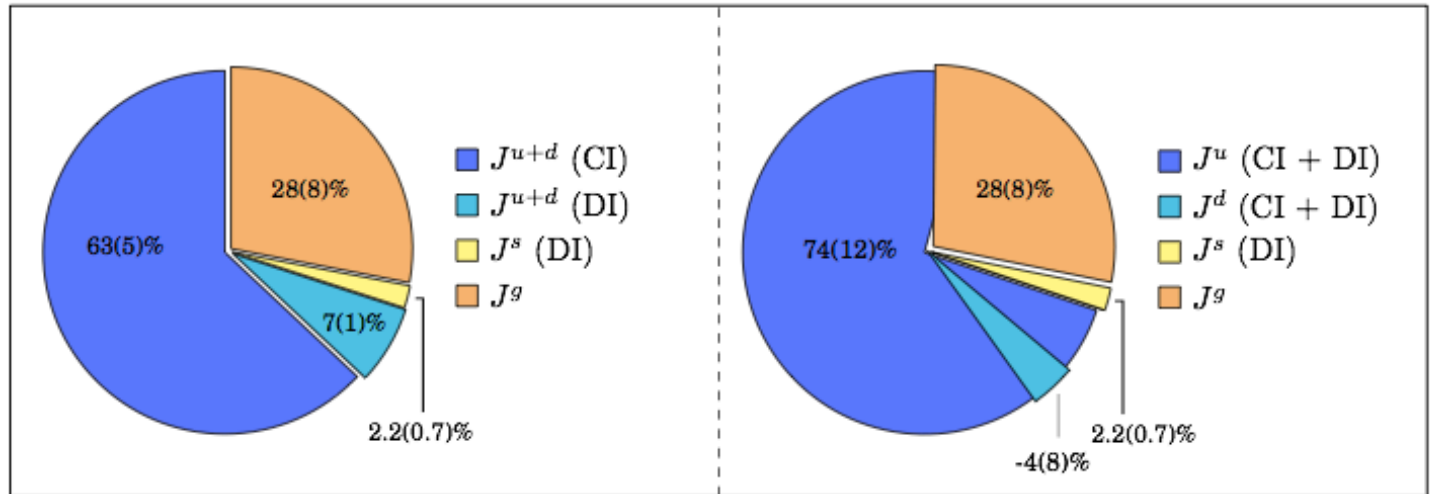
Nucleon spin and OAM from lattice QCD

□ χ QCD Collaboration:

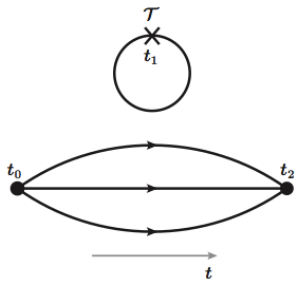
[Deka *et al.* arXiv:1312.4816]



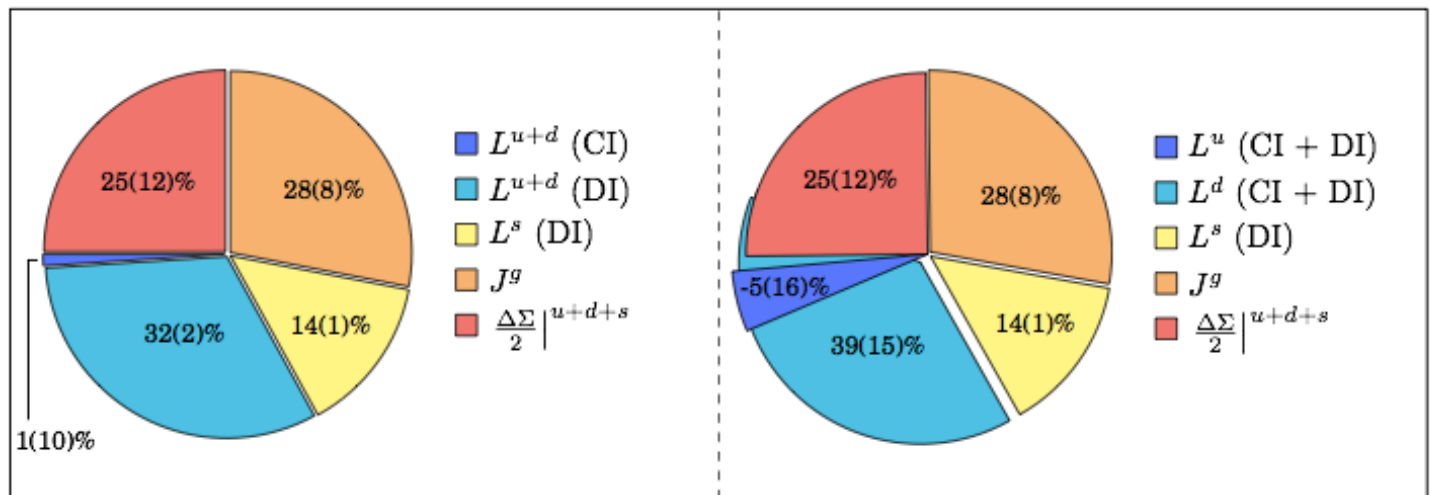
Connected
Interaction (CI)



(b)



Disconnected
Interaction (DI)



(c)

Connect OAM to observables

□ Difference between two OAM definitions:

Burkardt, 2008

$$\mathcal{L}^q - L^q = -g \int d^3x \langle P, S | \bar{q}(\vec{x}) \gamma^+ [\vec{x} \times \int_{x^-}^{\infty} dr^- F^{+\perp}(r^-, \mathbf{x}_{\perp})]^z q(\vec{x}) | P, S \rangle$$

Caused by the work done by the torque along the trajectory of q

Color Lorentz force: $\sqrt{2}F^{+y} = F^{0y} + F^{zy} = -E^y + B^x = -(\vec{E} + \vec{v} \times \vec{B})^y$ for $\vec{v} = (0, 0, -1)$

□ Connection to GPDs:

Ji, 96

Burkardt, 2001, 2005

$$\langle J_q^i \rangle = S^i \int dx [H_q(x, 0, 0) + E_q(x, 0, 0)] x$$

□ Quark canonical OAM to TMDs, GTMDs – model dependent:

$$\mathcal{L}_z = - \int dx d^2k_{\perp} \frac{\vec{k}_{\perp}^2}{2M^2} h_{1T}^{\perp}(x, \vec{k}_{\perp})$$

$$\ell_z = - \int dx d^2k_{\perp} \frac{\vec{k}_{\perp}^2}{M^2} F_{14}(x, 0, \vec{k}_{\perp}, \vec{0}_{\perp})$$

[Lorce, Pasquini (2012)]

Note:

**No gluons and
not QCD EOM !**

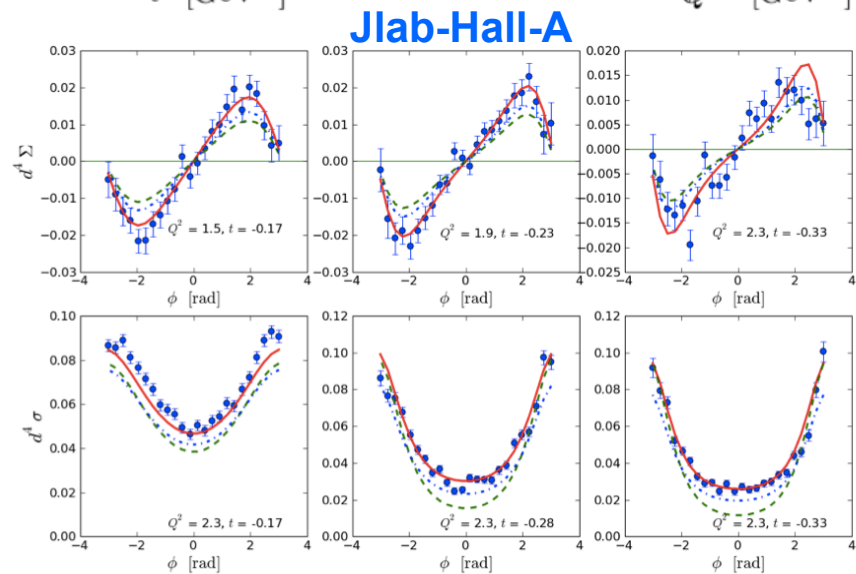
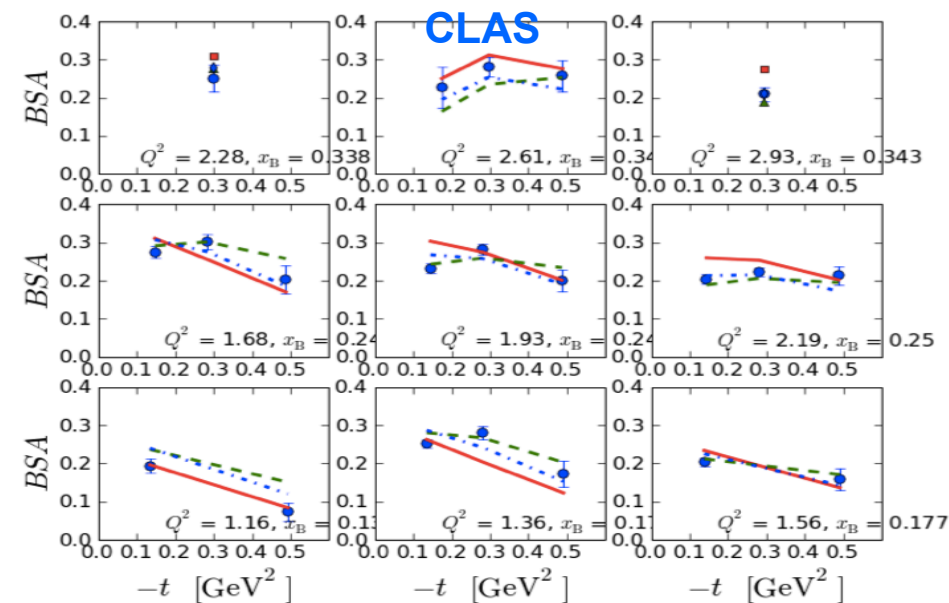
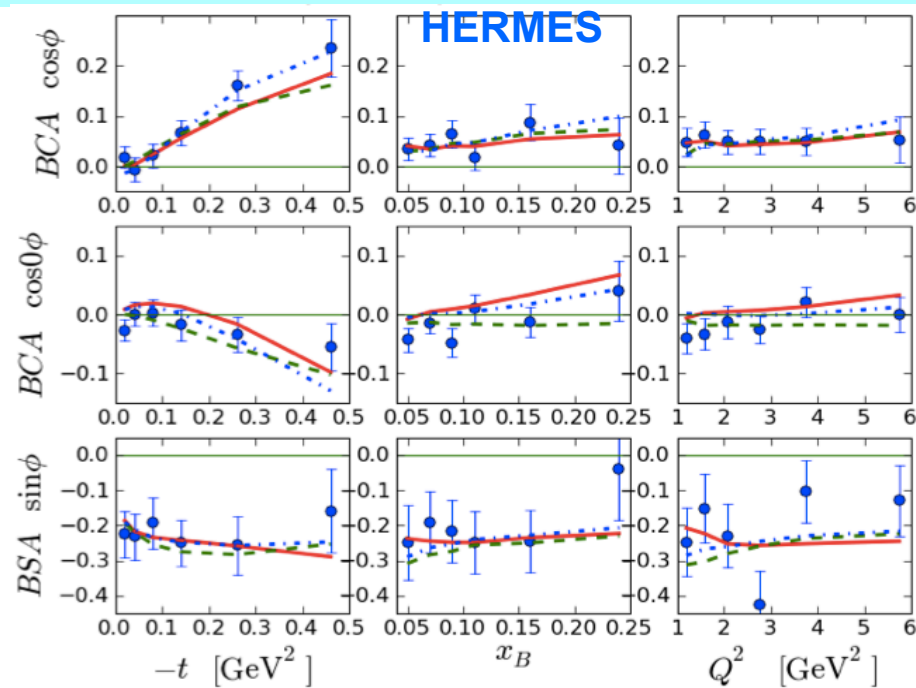
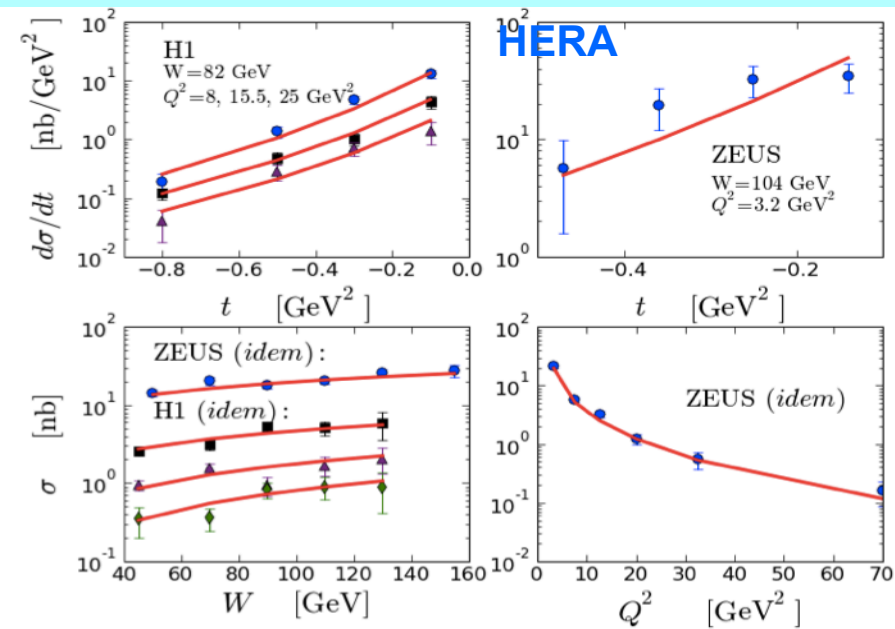
[Lorce, Pasquini (2011)]

[Lorce, et al (2012)]

[Kanazawa, et al (2014)]

Model	LCCQM			χ QSM		
	u	d	Total	u	d	Total
ℓ_z^q	0.131	-0.005	0.126	0.073	-0.004	0.069
L_z^q	0.071	0.055	0.126	-0.008	0.077	0.069
\mathcal{L}_z^q	0.169	-0.042	0.126	0.093	-0.023	0.069

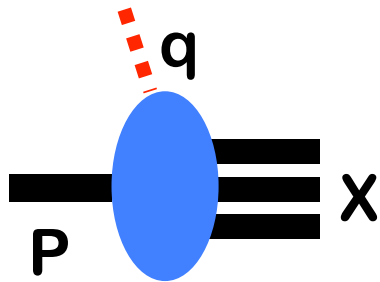
GPDs: just the beginning



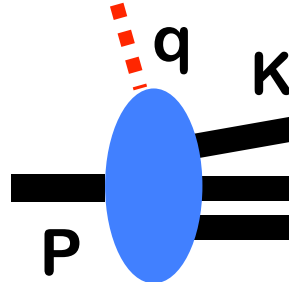
Structure vs collision dynamics

□ Probing nucleon structure (with/without breaking it):

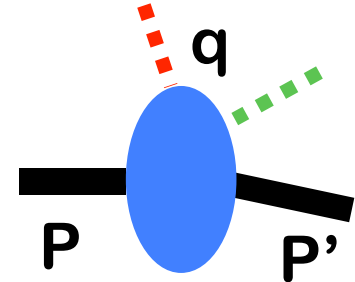
with a large momentum transfer ($-q^2 \gg 1/\text{fm}^2$): “see” quarks and gluons



Without looking
at the final-state

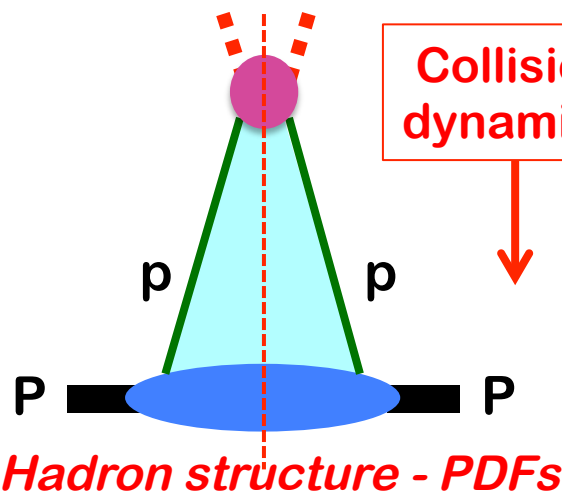


Measure the
final-state

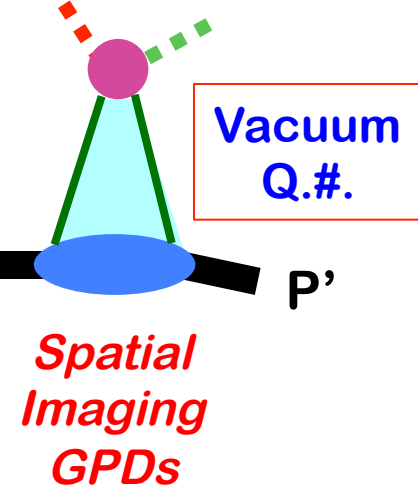
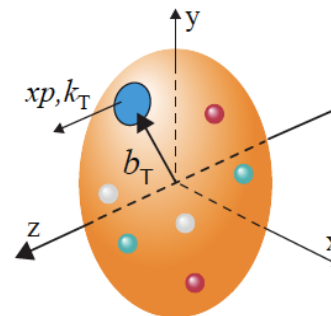
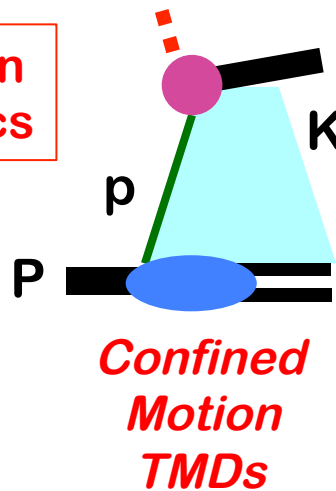


Keep the
hadron intact

□ Separating structure from collision dynamics – *Factorization*:



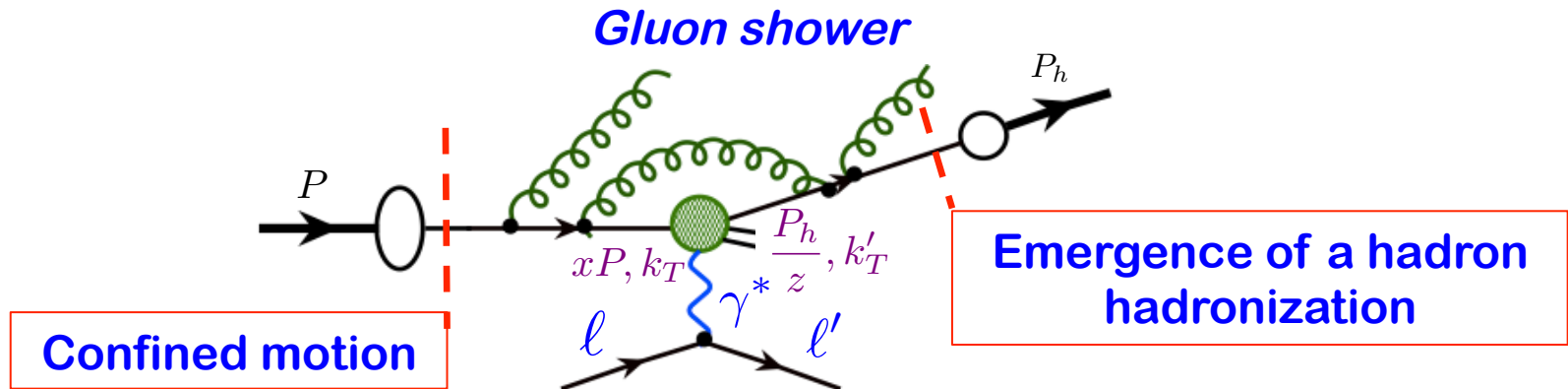
Collision
dynamics



Vacuum
Q.#.

Example: measured parton k_T

□ Sources of parton k_T at the hard collision:



□ Large k_T generated by the shower caused by the collision:

- ✧ Q^2 -dependence – **linear** equation of TMDs in **b-space**
perturbative at small b , but, not all b
- ✧ Solution – TMDs proportional to “input distribution” – boundary condition
 Q^2 -dependence of TMDs in k_T is sensitive to the “input”

□ “True” parton’s confined motion – more theory work needed:

- ✧ Separation of perturbative from nonperturbative – not as simple as PDFs
- ✧ $\ln(Q)$ -dependence of the “input” might get a large correction at low Q

TMDs are very interesting, SIDIS is the best place to measure!

The Future: Helicity distributions

□ Quark polarization – better determined:

✧ Quark polarization at $x \rightarrow 1$ – challenges – JLab12

□ Sea quark polarization – not well-determined:

✧ Polarized RHIC + SIDIS @ EIC

A sizable contribution to the proton spin
(~ 6%, current global fittings)

□ Gluon polarization – need small-x region:

✧ Inclusive DIS + SIDIS @ EIC

Current small-x technique for unpolarized gluon

Need to develop new technique to treat polarized small-x glue

□ Lattice QCD to calculate PDFs, not the moments:

✧ Quasi-PDFs ~ two-parton correlators along z-axis \neq PDFs

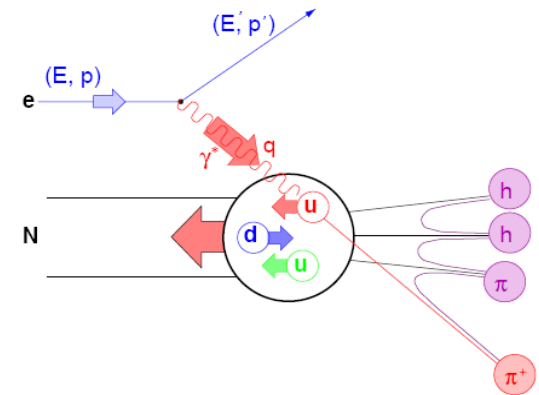
→ Normal PDFs as $P_z \rightarrow \infty$

Ji, Lin, et al. 2013

→ Factorized to Normal PDFs at a finite P_z

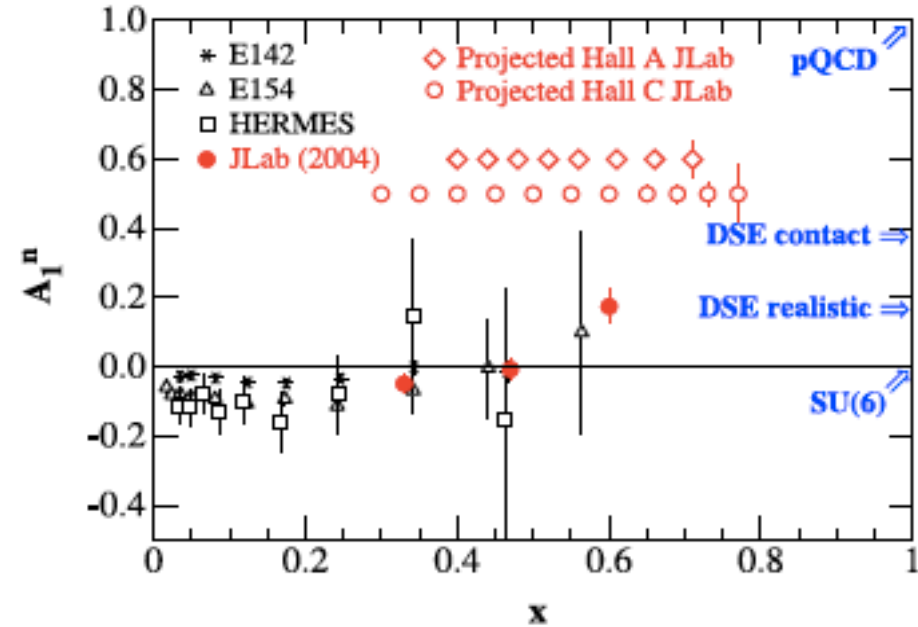
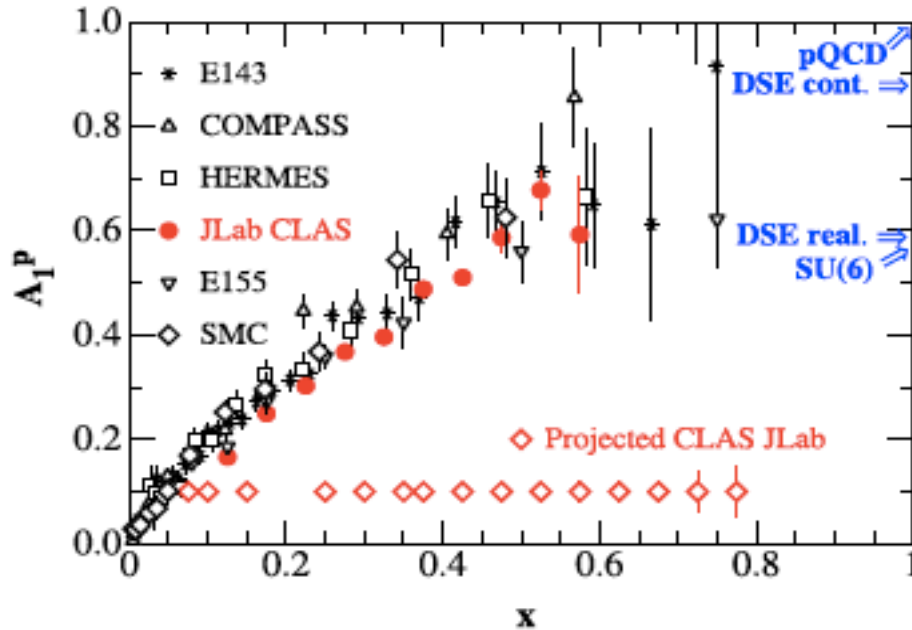
Ma, Qiu, 2014

Global analysis of lattice “data” for PDFs



Valence quark helicity at large x

□ JLab program:



	$\frac{F_2^n}{F_2^p}$	$\frac{d}{u}$	$\frac{\Delta d}{\Delta u}$	$\frac{\Delta u}{u}$	$\frac{\Delta d}{d}$	A_1^n	A_1^p
DSE-1	0.49	0.28	-0.11	0.65	-0.26	0.17	0.59
DSE-2	0.41	0.18	-0.07	0.88	-0.33	0.34	0.88
$0_{[ud]}^+$	$\frac{1}{4}$	0	0	1	0	1	1
NJL	0.43	0.20	-0.06	0.80	-0.25	0.35	0.77
SU(6)	$\frac{2}{3}$	$\frac{1}{2}$	$-\frac{1}{4}$	$\frac{2}{3}$	$-\frac{1}{3}$	0	$\frac{5}{9}$
CQM	$\frac{1}{4}$	0	0	1	$-\frac{1}{3}$	1	1
pQCD	$\frac{3}{7}$	$\frac{1}{5}$	$\frac{1}{5}$	1	1	1	1

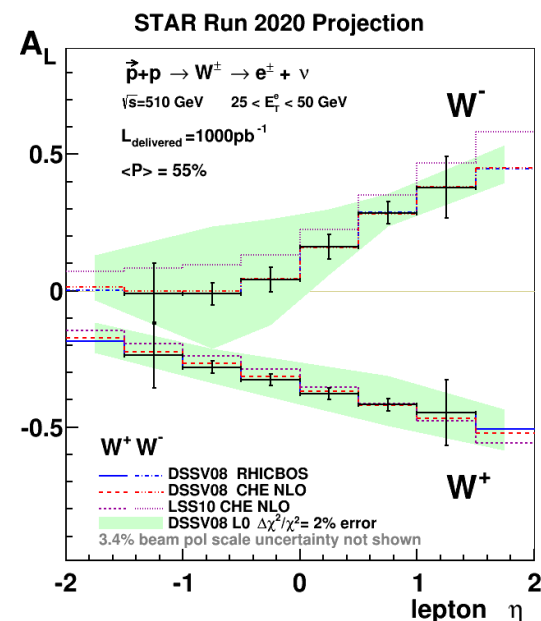
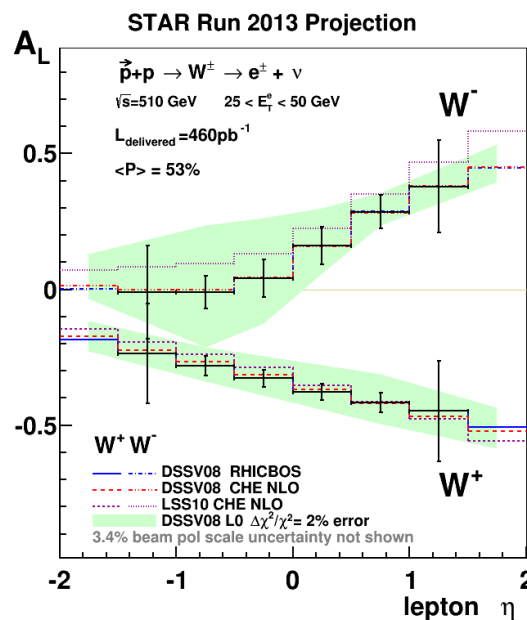
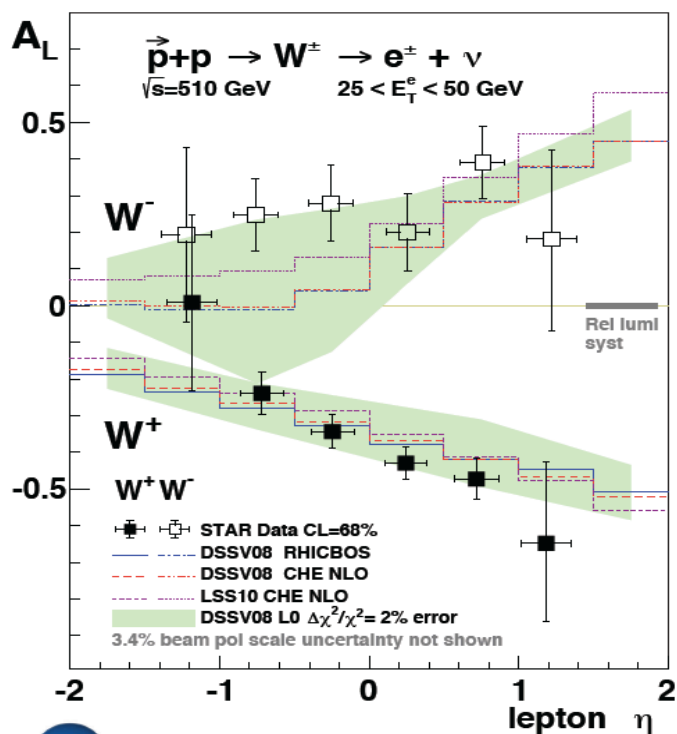
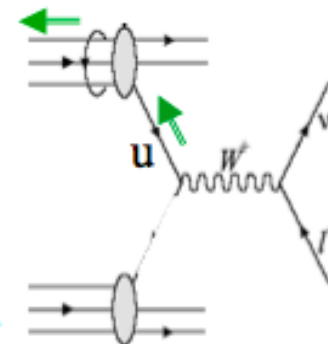
Sea quark helicity – RHIC program

□ Single longitudinal spin asymmetries:

$$A_L = \frac{[\sigma(+)-\sigma(-)]}{[\sigma(+)+\sigma(-)]} \quad \text{for } \sigma(s)$$

Parity violating weak interaction

Talks by Seidl, ...

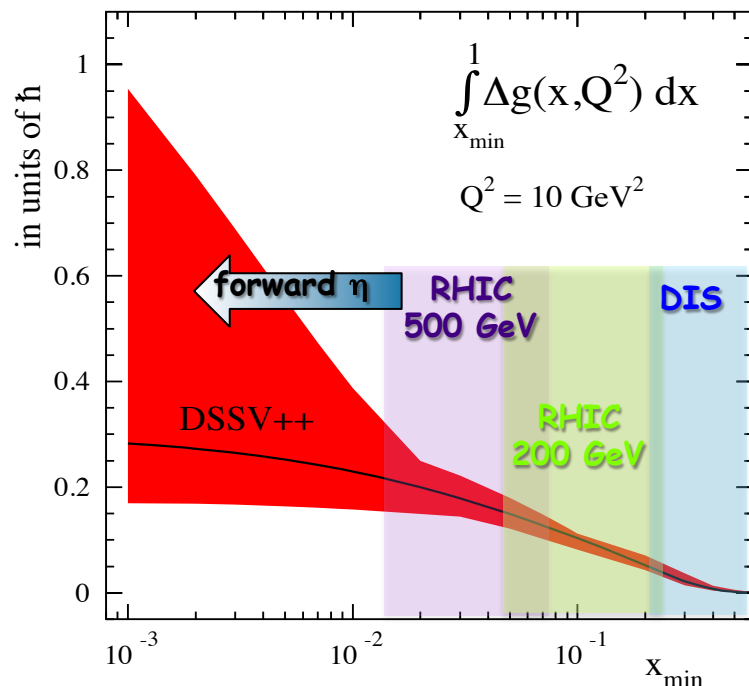


NEW arXiv:1404.6880

Sea quarks at medium/high x without target mass, HT, and FFs corrections!

Gluon helicity – RHIC program

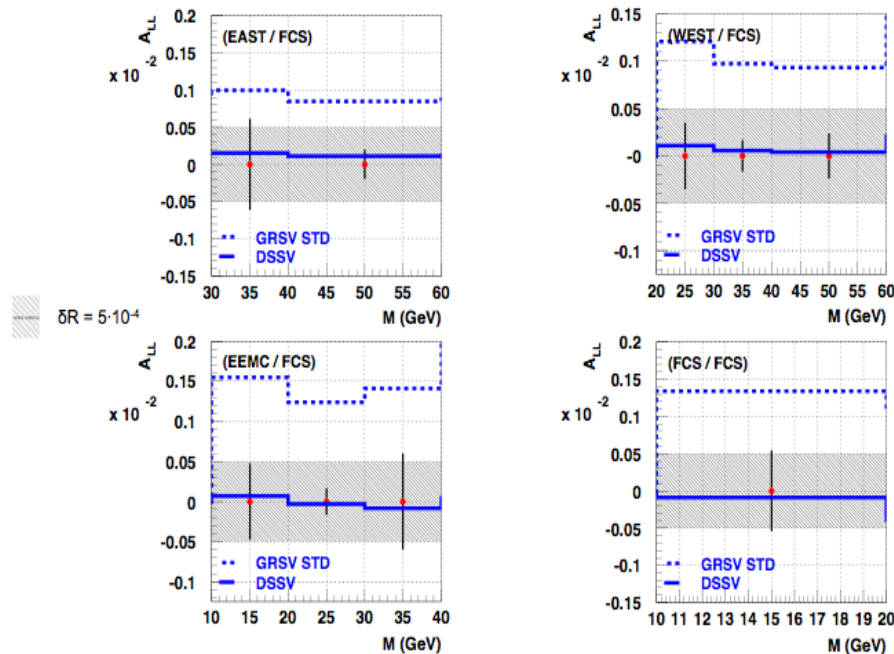
□ Go to the forward region:



Talks by Seidl, ...

$\sqrt{s} = 500 \text{ GeV}$

Delivered Luminosity = 1000 pb⁻¹
Polarization = 60%



$x : 0.01 \rightarrow 0.001$

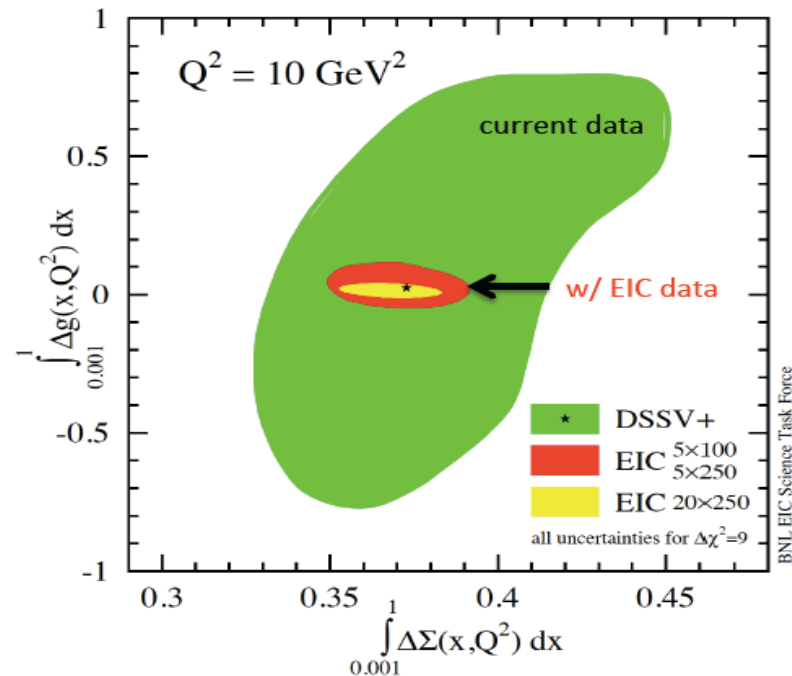
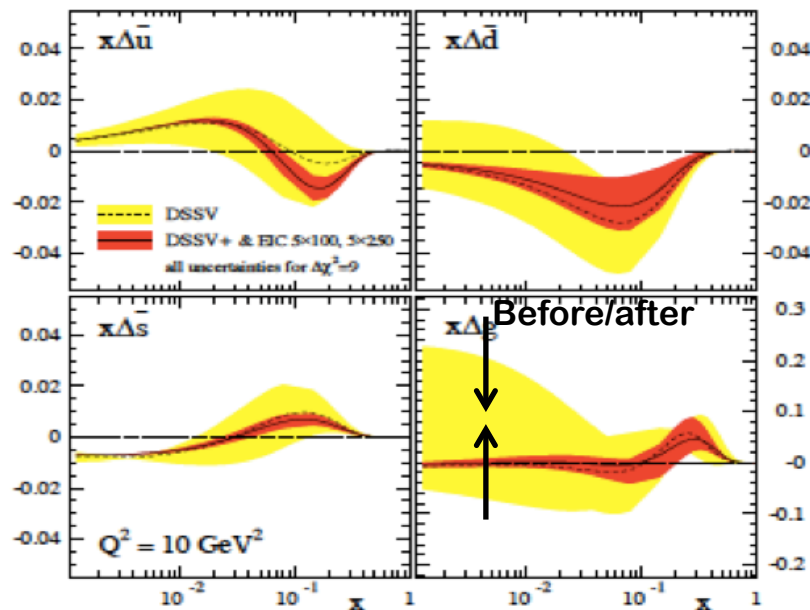
□ Theory:

- ✧ How to handle the small- x physics with polarized partons?
- ✧ How should the resummation of $\ln(1/x)$ powers be handled?

Helicity contribution to nucleon spin

□ One-year of running at EIC – the decisive measurement: See talk by Meiziani

Wider Q^2 and x range including low x at EIC!



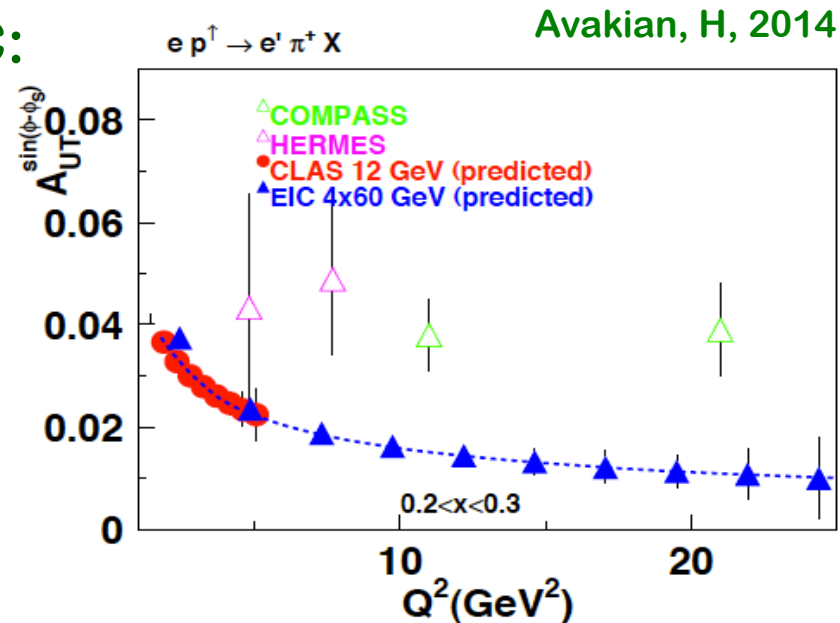
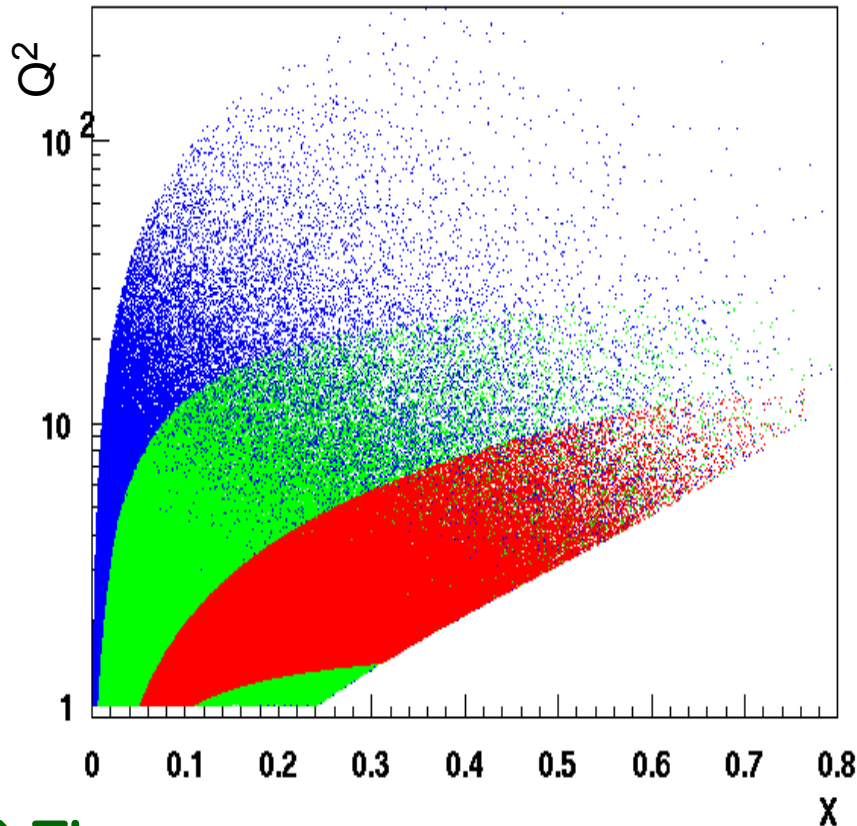
No other machine in the world can achieve this!

□ Ultimate solution to the proton spin puzzle:

- ✧ Precision measurement of $\Delta g(x)$ – extend to smaller x regime
- ✧ Orbital angular momentum contribution – measurement of GPDs!

The Future: TMDs, GPDs, and OAM

□ **Sivers TMD – from JLab12 to EIC:**



JLab@12GeV (25/50/75)

→ $0.1 < x_B < 0.7$: valence quarks

EIC $\sqrt{s} = 140, 50, 15$ GeV

→ $10^{-4} < x_B < 0.3$: gluons and quarks, higher P_T and Q^2 .

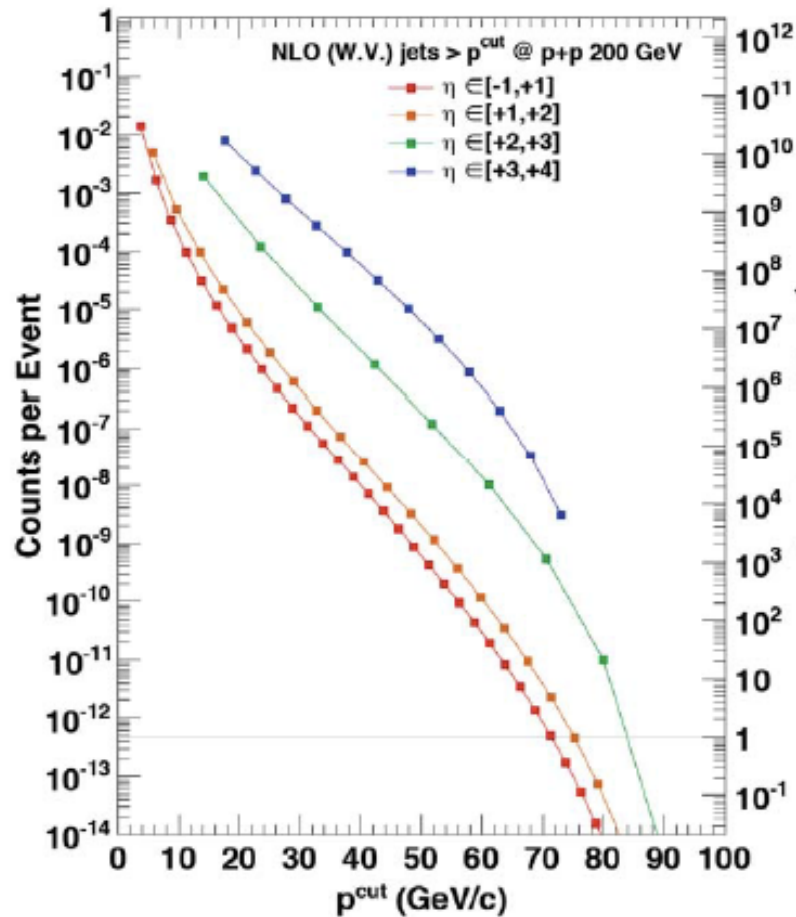
□ **Theory:**

- ✧ Theoretical control of Q^2 -evolution of TMDs, and its sensitivity on Non-perturbative input TMDs – confined parton motion in hadrons
- ✧ Any connection to orbital angular momentum?

The Future: TMDs, GPDs, and OAM

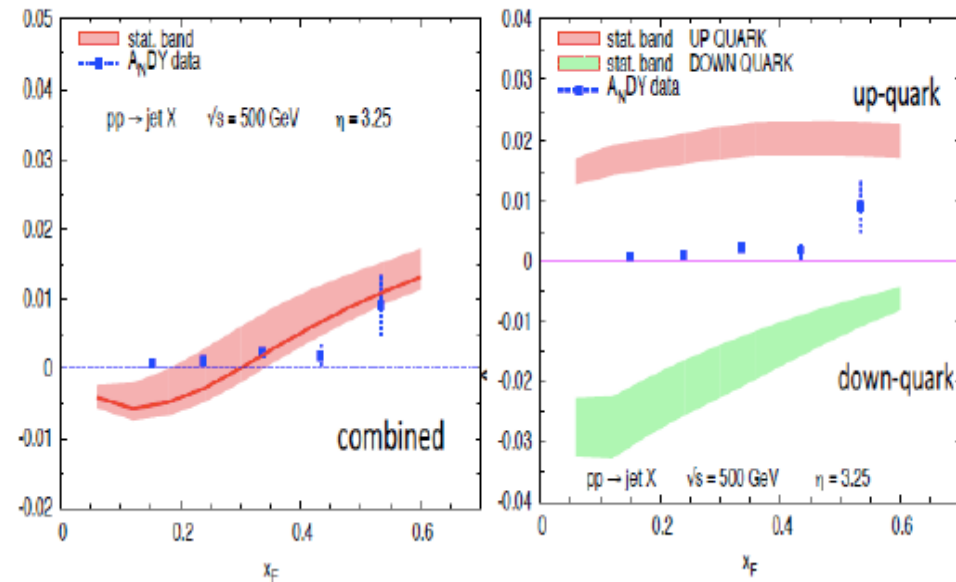
□ Siverson Effect – from fsPHENIX:

Lajoie, 2014



fsPHENIX Jet acceptance $1.7 < \eta < 3.3$
with anti- k_T $R=0.7$

Directly use Siverson function from SIDIS fit



□ Theory:

✧ TMD approach vs high twist collinear approach, and parton correlation!

The Future: TMDs, GPDs, and OAM

□ SoLId at JLab:

✧ Transversity:

Chiral-odd,
no coupling to gluon,
Transverse spin flip,
Least known PDFs...

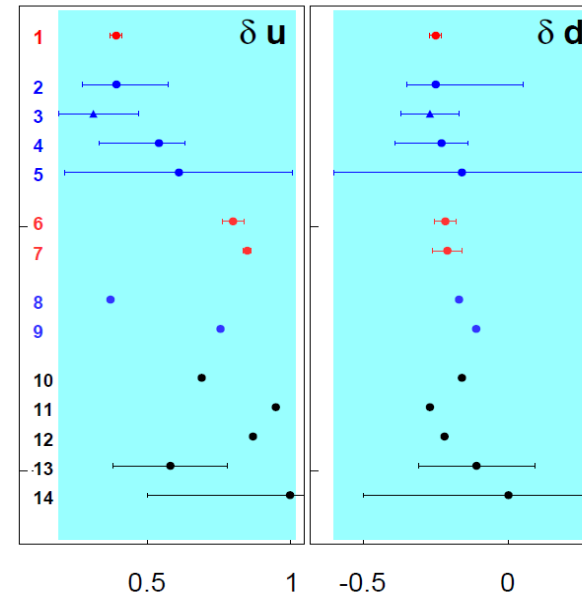
✧ Tensor charges:

Fundamental, many predictions

✧ Pretzelosity: TMD with $\Delta L=2$ ($L=0$ and $L=2$ interference)

Tensor Charges

J.P. Chen, 2014



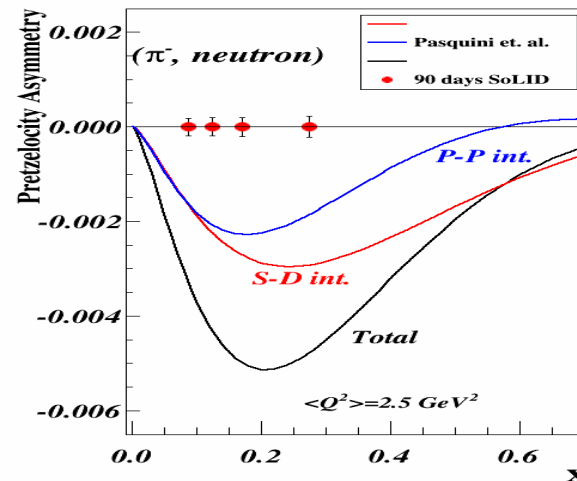
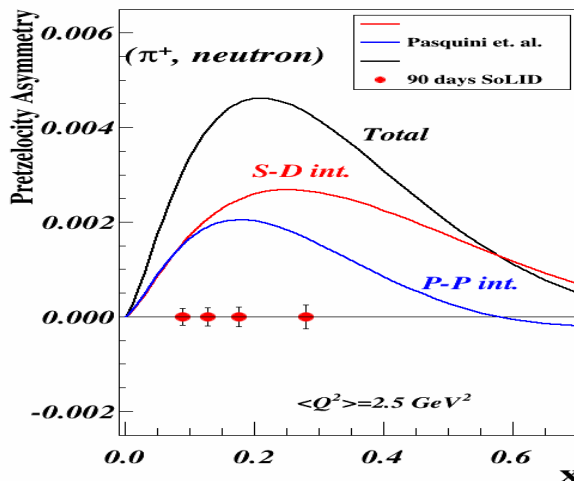
SoLID projections

Extractions from
existing data

LQCD

DSE

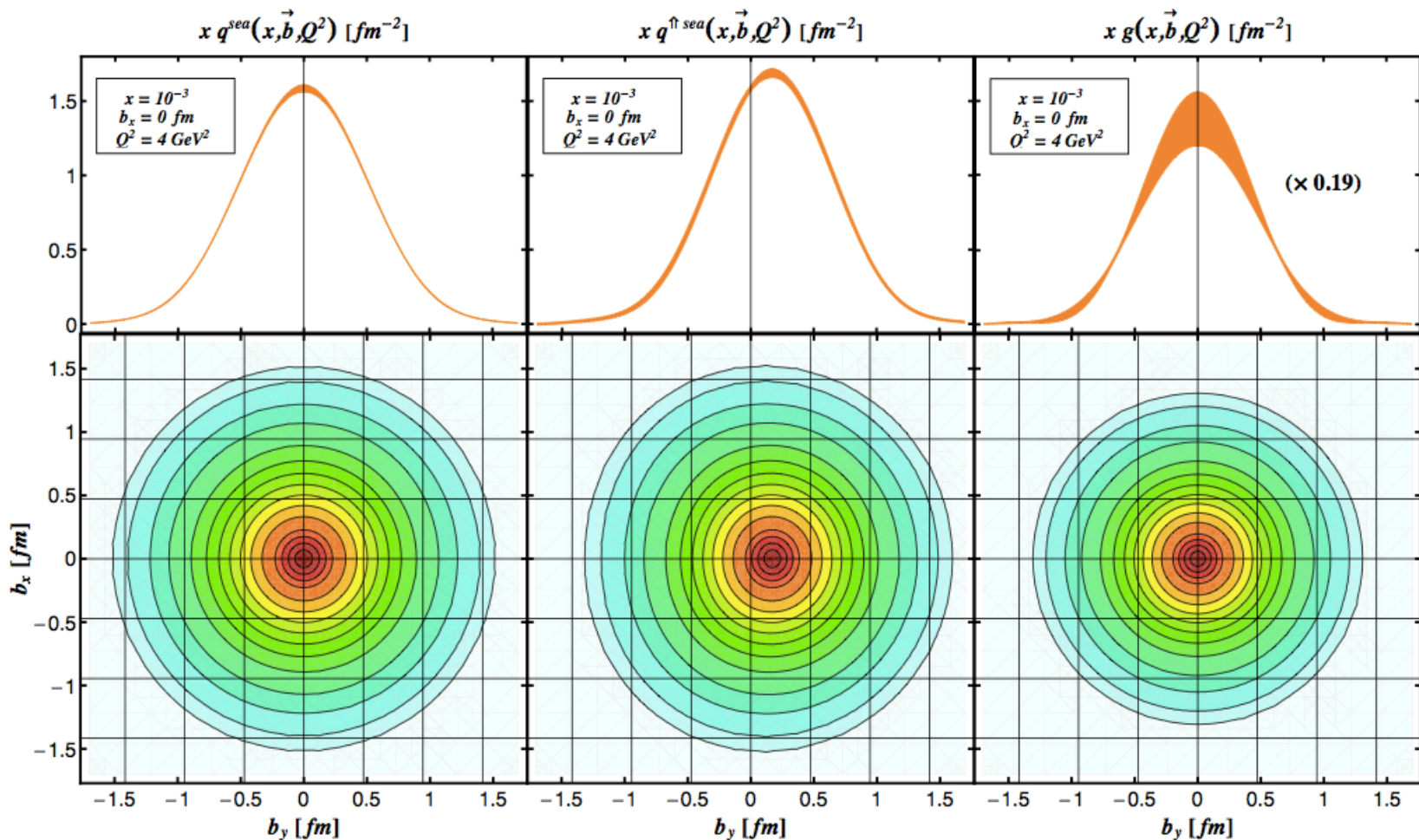
Models



Model relates
it to OAM

The Future: TMDs, GPDs, and OAM

□ GPDs: Spatial imaging:



$$q(x, |\vec{b}|, Q^2) = \frac{1}{4\pi} \int_0^\infty d|t| J_0(|\vec{b}| \sqrt{|t|}) H(x, \xi = 0, t, Q^2)$$



Quark radius?
Sea radius?
Gluon radius?

Summary

- ❑ After 40 years, we have learned a lot of QCD dynamics, but, only at very short-distance - less than 0.1 fm, and limited information on non-perturbative parton structure
- ❑ Understanding nucleon spin structure could provide **the first complete example** to describe the emerging hadron property from QCD dynamics
- ❑ Orbital angular momentum in QCD does not have a simple classical correspondence, since motion in QCD is always associated with phases and additional particles
- ❑ GPDs and TMDs are fundamental, and measurable with controlled approximation. They are necessary for getting a comprehensive 3D ``view'' of hadron's internal structure

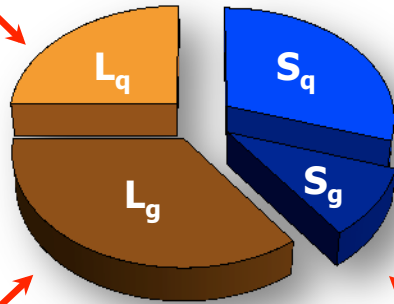
Thank you!

Backup Slides

Spin decomposition – Longitudinal polarization

$$\vec{\mathcal{L}}_q = \int d^3r \psi^\dagger [\vec{r} \times (-i\vec{\nabla})] \psi \quad \vec{\mathcal{S}}_q = \frac{1}{2} \int d^3r \psi^\dagger \vec{\Sigma} \psi$$

$n \cdot A = 0$
gauge

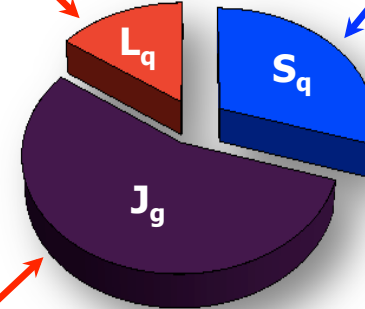


[Jaffe, Manohar (1990)]

$$\vec{\mathcal{L}}_g = \int d^3r E^{ai} [\vec{r} \times (-i\vec{\nabla})] A^{ai} \quad \vec{\mathcal{S}}_g = \int d^3r [\vec{E}^a \times \vec{A}^a]$$

$$\vec{\mathcal{L}}_q = \int d^3r \psi^\dagger [\vec{r} \times (i\vec{D})] \psi \quad \vec{\mathcal{S}}_q = \frac{1}{2} \int d^3r \psi^\dagger \vec{\Sigma} \psi$$

Gauge
invariance

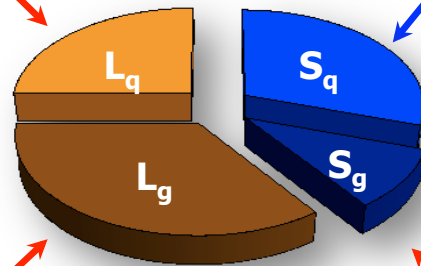


[Ji (1997)]

$$\vec{\mathcal{J}}_g = \int d^3r [\vec{r} \times (\vec{E}^a \times \vec{B}^a)]$$

$$\vec{\mathcal{L}}_q = \int d^3r \psi^\dagger \vec{r} \times (i\vec{D}_{\text{pure}}) \psi \quad \vec{\mathcal{S}}_q = \frac{1}{2} \int d^3r \psi^\dagger \vec{\Sigma} \psi$$

Gauge
Invariant
Extension
(GIE)



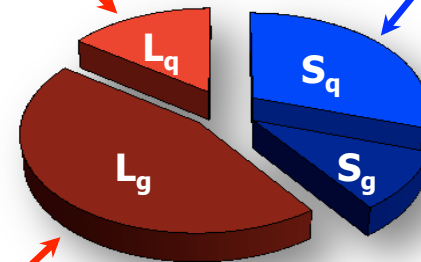
[Chen et al. (2008)]

$$\vec{\mathcal{L}}_q = \int d^3r E^{ai} \vec{r} \times \vec{D}_{\text{pure}} A_{\text{phys}}^{ai} \quad \vec{\mathcal{S}}_g = \int d^3r \vec{E}^a \times \vec{A}_{\text{phys}}^a$$

$$A = A_{\text{pure}} + A_{\text{phys}}$$

$$\vec{\mathcal{L}}_q = \int d^3r \psi^\dagger [\vec{r} \times (i\vec{D})] \psi \quad \vec{\mathcal{S}}_q = \frac{1}{2} \int d^3r \psi^\dagger \vec{\Sigma} \psi$$

Gauge
Invariant
extension



[Wakamatsu (2010)]

$$\vec{\mathcal{L}}_g = \int d^3r \vec{r} \times (\vec{E}^a \times \vec{B}^a) - \int d^3r \vec{E}^a \times \vec{A}_{\text{phys}}^a \quad \vec{\mathcal{S}}_g = \int d^3r \vec{E}^a \times \vec{A}_{\text{phys}}^a$$

Spin decomposition – Longitudinal polarization

❑ **Not unique:**

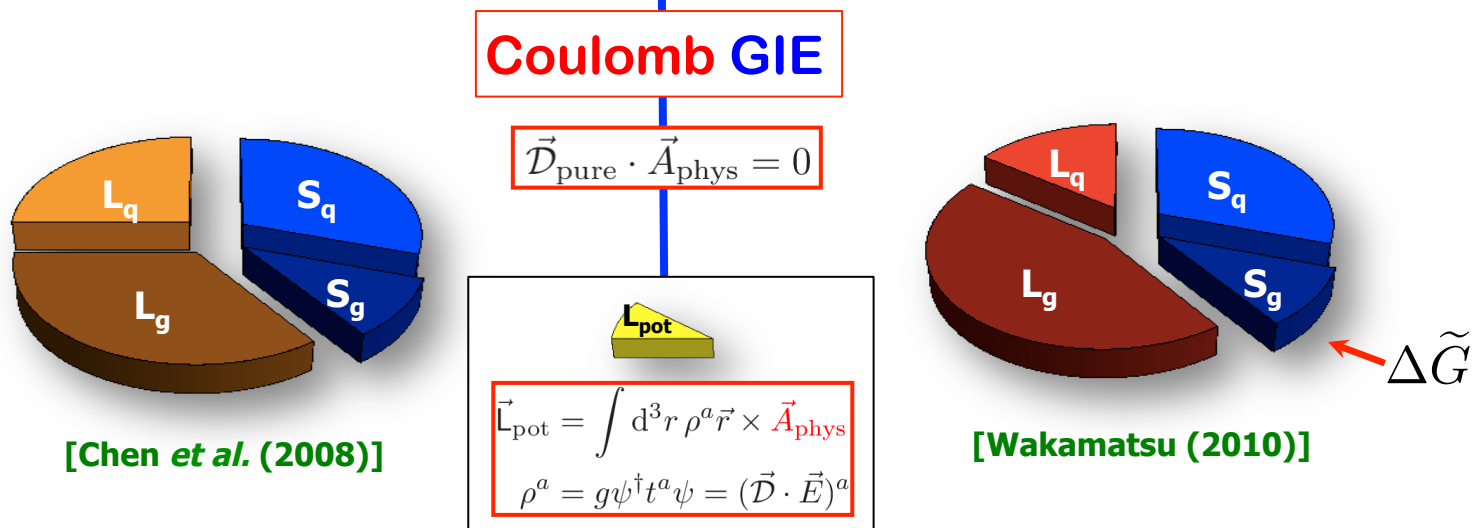
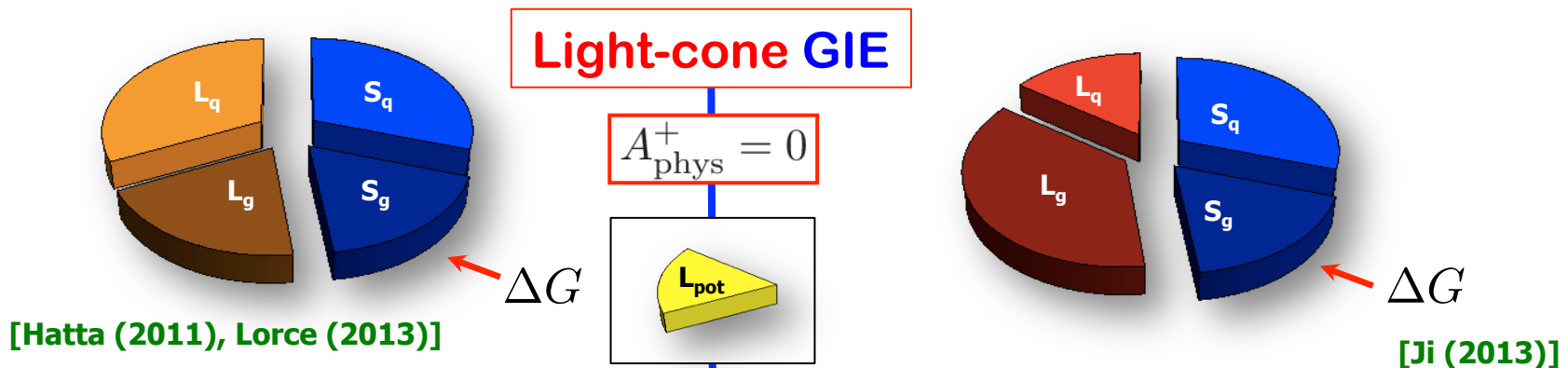
Stueckelberg symmetry

$$A = A_{\text{pure}} + A_{\text{phys}} = \underbrace{\bar{A}_{\text{pure}}}_{A_{\text{pure}} + C} + \underbrace{\bar{A}_{\text{phys}}}_{A_{\text{phys}} - C}$$

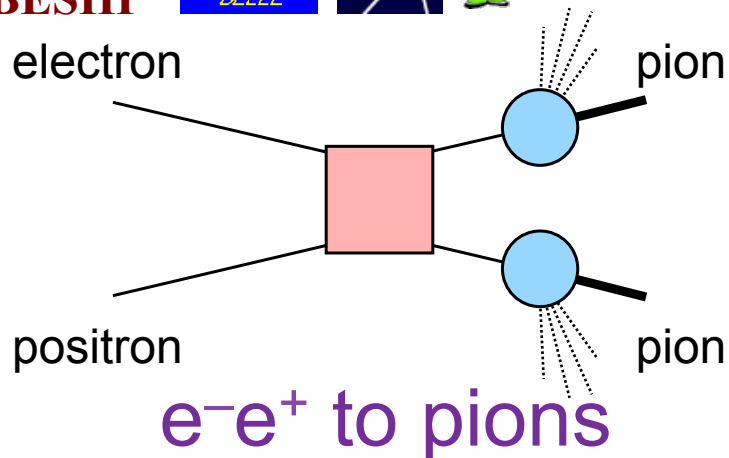
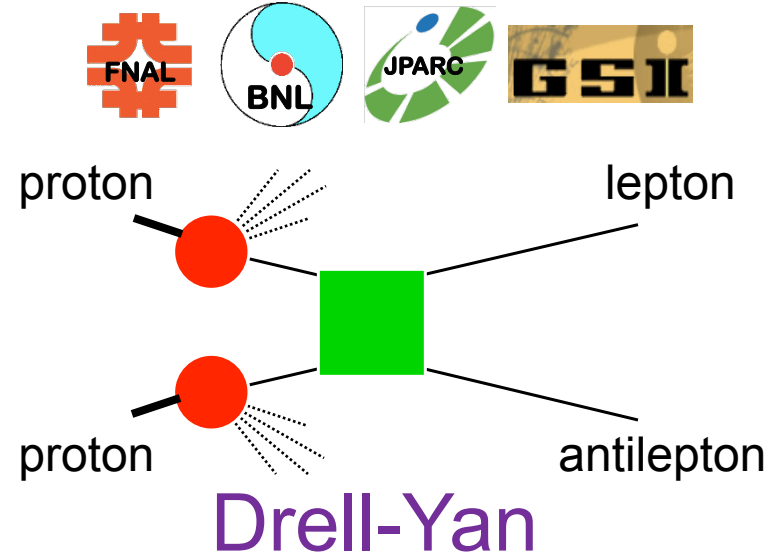
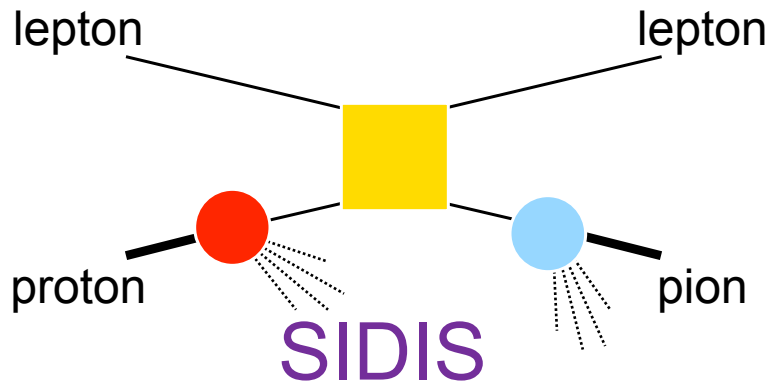
[Stoilov (2010)]

[Lorce (2013)]

Infinitely possibilities!



World effort on TMDs



- Partonic scattering amplitude
- Fragmentation amplitude
- Distribution amplitude

Test of the sign change!

$$f_{1T}^{\perp q}(\text{SIDIS}) = -f_{1T}^{\perp q}(\text{DY})$$

$$h_1^{\perp}(\text{SIDIS}) = -h_1^{\perp}(\text{DY})$$